Stabilizing effect of flexibility in the wake of a flapping foil

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The wake of a flexible foil undergoing pitching oscillations in a low-speed hydrodynamic tunnel is used to examine the effect of chordwise foil flexibility in the dynamical features of flapping-based propulsion. We compare the regime transitions in the wake with respect to the case of a rigid foil and show that foil flexibility inhibits the symmetry breaking of the reverse Bénard–von Kármán wake reported in the literature. A momentum balance calculation shows the average thrust to be up to three times greater for the flexible foil than for the rigid foil. We explain both of these observations by analysing the vortex dynamics in the very near wake.

Key words: flow-structure interactions, swimming/flying, vortex streets

1. Introduction

In nature, wings and fins are compliant structures (see e.g. Daniel & Combes 2002 and references therein). During locomotion, these flapping appendages endure deformation, actively or passively, which has an important role in the propulsive and manoeuvring capabilities of swimming (Fish 1999) and flying animals (Wootton 1992). A vast amount of work studying the effect of wing compliance in flapping wing systems has been reported in the literature (see Shyy et al. 2010 for a review), and it is clear that the redistribution of aerodynamic forces resulting from wing deformation can have a dramatic effect on performance. Chordwise flexibility, in particular, has been shown to increase the propulsive efficiency in various configurations of flapping-based propulsion (see e.g. Katz & Weihs 1978; Heathcote & Gursul 2007a; Thiria & Godoy-Diana 2010), and a few fluid physics mechanisms behind the beneficial effects of passive compliance for propulsive performance have been identified (Eldredge & Pisani 2008; Spagnolie et al. 2010; Ramanarivo, Godoy-Diana & Thiria 2011). In this paper we show that, aside from its well-documented effect on the thrust force, chordwise flexibility plays an important role in the stability of the propulsive wake. It has been shown in the literature that the mean propulsive jet produced by flapping motion can sometimes lose its symmetry, giving rise to a deflected jet (Jones, Dohring & Platzer 1998; Lewin & Haj-Hariri 2003; Heathcote & Gursul 2007b; Buchholz & Smits 2008; von Ellenrieder & Pothos 2008; Godoy-Diana, Aider & Wesfreid 2008; Cleaver, Gursul & Wang 2010; Godoy-Diana et al. 2009; Yu, Hu & Wang 2012). The mechanism of deflection is triggered by the wake vortices being shed as dipolar

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structures, instead of as the regular array of counter-rotating vortices of the reverse Bénard–von Kármán pattern characteristic of propulsive wakes produced by flapping motion. For the case of a rigid teardrop-shaped foil undergoing pitching oscillations, the phase space for the transition between different regimes has been well established in previous work (Godoy-Diana et al. 2008, 2009; Marais 2011). We examine here the effect of introducing flexibility to the problem, performing a detailed comparison of the vortex dynamics in the near wake of the flapping foil for two cases: the rigid foil (our benchmark case), and a flexible foil with the same shape but made of a compliant material. In addition to quantifying the increase in the thrust force observed when using a flexible foil, we demonstrate that flexibility inhibits the symmetry breaking of the propulsive wake.

2. Experimental set-up and parameters

The experimental set-up closely resembles the one described in Godoy-Diana et al. (2008) and consists of a pitching foil of span-to-chord aspect ratio of 4:1 placed in a hydrodynamic tunnel (see figure 1). The motion of the foil is driven by a stepper motor and has been set to a triangular wave of varying frequencies and amplitudes. The control parameters on the experiment are the flow velocity in the tunnel \( U \) and the foil oscillation frequency \( f \) and pitching angle \( \theta \). The latter determines a peak-to-peak amplitude of oscillation of the trailing edge that we define as \( A \) in the case of the rigid foil. As will be discussed below, the actual displacement of the trailing edge \( A_{\text{eff}} \) equals \( A \) for the rigid foil but varies depending on the frequency for the flexible foil. We define the following non-dimensional parameters: the Reynolds number \( Re = Uc/\nu \) based on the foil chord \( c \), where \( \nu \) is the kinematic viscosity, fixed to \( Re \approx 1035 \) in the present experiments. The dimensionless effective flapping amplitude \( A_D = A_{\text{eff}}/D \), and a Strouhal number \( St_D = fD/U \), both defined using the foil width \( D \) as characteristic length scale. It has recently been shown (Godoy-Diana et al. 2008) that this three-parameter description is needed to allow for a proper characterization of the transitions in the wake.
The deformation experienced by the flexible foil while flapping can be characterized using the actual amplitude $A_{\text{eff}}$ (peak-to-peak amplitude measured at the trailing edge of the foil), which is larger than the amplitude $A$ that would be observed with a rigid foil for a given angular oscillation. The ratio $A_{\text{eff}}/A$ thus increases with the flapping frequency for a given value of the imposed rigid amplitude $A$ (see figure 2, where a schematic diagram of this effect is also shown). The latter observation holds for the regime considered in the present study, but one could probably find other regimes where $A_{\text{eff}}/A < 1$. This is related to the problem of an optimal flexibility (see e.g. Michelin & Llewellyn Smith 2009) as a function of the forcing frequency of a flapping foil. The amplitude-based Strouhal number $St_A = St_D \times A_D$ that is usually found in the literature was in the range $0.05 < St_A < 1.2$ in the present experiments.

Time-resolved measurements were performed using two-dimensional particle image velocimetry (PIV) on a plane probing the flow around the foil at mid-span. A continuous wave laser (DPSS 2W at 532 nm) and a cylindrical lens were used to produce a light sheet of $\approx$1 mm width in the whole imaging region ($\approx$10.4D to 26.6D and $\pm$10.8D in the $x$ and $y$ directions, respectively). Each recording consisted of 2100 images sampled at 500 Hz using a Phantom V9.1 camera with a resolution of 1600 $\times$ 1200 pixels. The flow was seeded with 20 $\mu$m polyamide particles. The PIV computation and post-processing were done using a LaVision system as well as MATLAB and the PIVMat Toolbox (Moisy 2007). The PIV calculation was performed with 16 $\times$ 16 pixel interrogation windows with a 50% overlap, giving a resolution of one vector every 0.7 mm.

We investigate two cases, using foils with the same geometry and dimensions (indicated in figure 1), but differing in their structural material. The first one, already used in previous studies, is made of acrylic glass and will be referred to as the rigid foil in the following. The second one, the flexible foil shown in figure 1, is made of a silicone elastomer material (vinyl polysiloxane), cross-linked with a curing agent to obtain a Young’s modulus of $E \approx 30$ kPa.
FIGURE 3. (Colour online) Amplitude versus frequency phase diagram for the transitions in the wake for (a) the rigid foil (see also Godoy-Diana et al. 2009) and (b) the flexible foil. Inserted images correspond to a typical mean horizontal velocity field for each regime. Solid and dashed lines correspond to transitions between regimes (see text). For the flexible case, the transition that marks the symmetry breaking of the reverse Bénard–von Kármán wake is not observed. (c–f) Snapshots of typical vorticity fields for each regime.

which, although beyond the scope of the present work, remains to be explored experimentally.

3. Transitions in the wake

A description using the frequency and amplitude of the oscillatory motion as independent parameters has recently been shown to be the optimum framework to fully characterize the quasi-two-dimensional (Q2D) regimes observed in the wake of a pitching foil (Godoy-Diana et al. 2008; Schnipper, Andersen & Bohr 2009). The phase diagram indicating the regime transitions for the rigid foil in a \((St_D, A_D)\) map is recalled in figure 3(a), where a typical snapshot of the mean horizontal velocity field is shown for each region of the phase space (snapshots of a typical vorticity field for each case are shown below in figure 3c–f). The solid line marks the transition between a Bénard–von Kármán type (BvK) wake (where the mean flow presents a velocity deficit behind the foil) and the reverse BvK wake characteristic of propulsive regimes (where the mean flow is a jet). The broken line locates the symmetry breaking of the reverse BvK street that occurs when two successive vortices are shed too close to each other, the closeness being determined by a ratio of the flapping and advective time scales (see Godoy-Diana et al. 2009).

The effect of adding flexibility to the flapping foil modifies the structure of the flow in the wake and thus the transition map (see figure 3b). While there is no observable effect on the transition between the BvK and reverse BvK regimes (i.e. the solid line does not move appreciably between figures 3a and 3b), the symmetry breaking of the BvK street is inhibited for the flexible foil in the range of parameters explored. The
propulsive jet that is deflected for the rigid foil (in the top right region of the $(St_D, A_D)$ parameter space in figure 3a) stays symmetric in the case of the flexible foil. This can be observed in more detail in the comparison of the mean horizontal velocity profiles for a specific point of the parameter space shown in figure 4.

A standard momentum balance using the mean velocity field permits us to estimate the average thrust force (see Godoy-Diana et al. 2008). Figure 4 shows the mean drag coefficient $C_D/C_D0$ surfaces in the $(St_D, A_D)$ map for the two foils. As mentioned in Godoy-Diana et al. (2008), the drag–thrust transition (the solid contour where $C_D = 0$) happens after the transition from the BvK to the reverse BvK regime. This observation has been confirmed by Bohl & Koochesfahani (2009), who used an alternative control volume analysis that takes into account the streamwise velocity fluctuations and the pressure term. We recall that for a given angular amplitude $\theta$ of the pitching motion, at equal flapping frequency the effective amplitude has been observed in the present experiments to be larger for the flexible foil than for the rigid one. Now if we compare two points in the parameter space at equal effective amplitudes (i.e. equal $A_D$), the calculated forces for the flexible and the rigid foils are indeed similar (see the contours in figure 4). Seeking to characterize the effect of flexibility, however, one should...
consider the pitching motion as the input and the passive deformation of the foil as an effect, which would mean comparing points of equal angular amplitude $\theta$ (e.g. the square marker in figure 4) where the propulsive force is significantly larger for the flexible foil. Comparing forces between the rigid and the flexible foils at equal values of angular pitching amplitude, we can see that the thrust force for the flexible foil can be up to three times larger than the values obtained with the rigid foil, a feature that seems to be mainly determined by the increase in effective flapping amplitude resulting from the foil deformation.

The present experiments have thus demonstrated that foil flexibility has an effect on both the thrust force produced by the foil and the symmetry properties of the wake. In what follows we attempt to gain a better understanding of the mechanisms responsible for these observations, focusing on the formation of vortices in the case of the reverse BvK wake, where the vorticity generated at the leading edge and along the boundary layer on each side of the flap merges with the tip vortex at the trailing edge, and is shed as a single structure each half period of oscillation. The interest in the early stages of the vortex formation process is twofold. First, because vortices are formed in the vicinity of the oscillating foil, it is during these first stages that their influence or footprint on the production of hydrodynamic forces will be greatest. Second, it has been shown that the symmetry properties of the wake are driven by the dynamics of the very near wake, where the formation of dipolar structures is the mechanism that triggers the symmetry breaking of the reverse BvK vortex street.

4. Vortex dynamics

For each experimental configuration, we start tracking the vortex closest to the trailing edge at the moment of reversal in the direction of the flapping motion, which corresponds to the birth of the new vortex. The vortex is characterized in terms of its circulation and streamwise and transverse position in the wake, as in Godoy-Diana et al. (2009). In figure 5, a time series of vorticity fields is shown for each type of foil, rigid and flexible, for the same control parameters: frequency ($St_D = 0.3$) and pitching angle ($\theta = 7.5^\circ$). The two vortices closest to the flap (counter-rotating, enclosed by squares in figure 5) are tracked, giving the time series of position shown in figure 6.
We will refer to the vortex closest to the flap (negative vorticity) as vortex I and the one shed previously (positive vorticity) as vortex II. The first point concerns the time evolution of the streamwise position of the vortices: we observed systematically that in the case of the flexible foil, vortices are shed closer to the origin (the rotation axis of the foil) in the $x$ direction than in the case of the rigid foil (this can be seen in the track of vortex I in figure 6). The difference between the two foils is less marked in the track of vortex II. The tracks of the $y$ position (figure 6) show the wake deflection observed for the rigid foil in this case, while in the case of the flexible foil the vortices are shed symmetrically.

The difference between the $x$ position of vortex I in the rigid and flexible cases can be understood considering the deformation experienced by the flexible foil during the vortex formation process: when the flap changes the direction of motion, because of the foil deformation the tip position moves closer to the origin and so does the shed vortex. It follows from this observation that the two consecutive vortices of opposite sign shed at each flapping period are closer in the rigid case than in the flexible case, as illustrated in figure 7. Recalling that the symmetry breaking in the wake directly depends on the relative self-advection velocity of the first dipolar structure in the near wake of the foil (Godoy-Diana et al. 2009), the fact that flexibility keeps the newly shed vortex (vortex I) from being shed close enough to vortex II to form a vortex pair can explain the observed inhibition of the deflected wake.

We now study the temporal evolution of the circulation during vortex formation. We define the time origin as the moment when the foil changes direction, which triggers the shedding of a vortex into the wake and marks the beginning of the growth process of a new vortex at the trailing edge of the foil. The circulation grows in time and rapidly tends toward a maximum value that remains relatively constant even after the next change in direction (which restarts the formation process for the next opposite-signed vortex). This evolution can be seen in figure 8. If we compare this circulation evolution for flexible and rigid foils, it appears clearly that the vortex in the wake of the flexible foil forms faster than in the case of the rigid foil.
(a) 

(b) 

Figure 7. (Colour online) Vorticity field in the near wake for (a) the rigid foil and (b) the flexible foil. The dashed lines mark the horizontal distance between the centres of two consecutive vortices in the rigid case, pointing out the larger distance between the two vortices in the flexible case. The self-advection velocity of the dipolar structure $U_{dipole}$ is shown schematically in both cases, larger in the rigid case where the dipole is more compact.

The link between vortex formation time and the force experienced by the foil can be qualitatively understood using the simple approach proposed by Protas & Wesfreid (2003) for a two-dimensional wake vortex street, starting from the impulse formula that associates the force with the time derivative of the vorticity impulse (see e.g. Saffman 1992) $F = -d/dt \int_{\Omega} (r \times \omega) d\Omega$, where the fluid density is set to unity, the flow domain $\Omega$ extends to infinity, $r = [x, y]$ is the position vector, $\omega = (\partial_x v - \partial_y u) \hat{k}$ is the vorticity, $u$ and $v$ are the two velocity components, and $\hat{k}$ is the unit vector perpendicular to the plane of motion. Considering a vortex street modelled by point vortices, the projection of the impulse formula along the $x$ axis gives the following approximate expression for the drag force, $F_D \approx -d/dt \sum_i \Gamma_i \Delta y_i$, where $i$ denotes the $i$th vortex in the wake and $\Delta y_i$ its distance to the wake centreline. The hydrodynamic force is thus intimately linked to the spatial arrangement of vortices in the wake as well as to their sign and intensity. The other important point is that this unsteady contribution to the force coming from the vortices depends on the temporal evolution of the circulation. Considering the comparison between the rigid and flexible foils of the present experiments, the faster formation of each vortex in the case of the flexible foil is therefore consistent with the observed increase in the propulsive force.

In order to shed some light on the physical mechanism that determines the faster formation of vortices in the wake of the flexible foil, we examine the velocity field in
the near wake. In figure 9 we compare the velocity profile $|V(t)|$ at the trailing edge of the foil for both cases (along the white line represented on the absolute velocity fields in figure 9a), at four different instants distributed over one foil oscillation period. The profiles for the rigid and flexible foils are similar, but a distinctive feature appears when the foil changes direction of oscillation ($4/12T$ and $10/12T$): the velocity jet near the tip of the foil is clearly more intense in the case of the flexible foil. The faster growth of the vortex circulation observed in figure 8 can therefore be explained by acknowledging that the flexible foil curvature enhances the flow around the trailing edge of the foil, locally accelerating the fluid that will feed the growing vortex.

We may also note that this is compatible with another point observed in the previous section: in the flexible case, once the newly formed vortex is released into the wake it accelerates and catches up its delay with respect to the case of the rigid foil (see the x
position of vortex II for both cases in figure 6). This transient faster initial advection velocity of the vortices can be explained by the deformation dynamics of the flexible structure: in the manner of a spring, after reaching its maximum deformation the foil structure comes back to its initial shape, contributing to acceleration of the fluid in the near wake.

5. Concluding remarks

We have shown that adding flexibility plays a strong dynamical role in the wake produced by a flapping foil. On the one hand, the effective amplitude obtained passively due to the deformation of the flexible foil while flapping (figure 2) leads to an increase in the propulsive force with respect to the case of the rigid foil (figure 4). On the other hand, the interaction of the shed vortices with the flexible structure inhibits the triggering of the symmetry breaking of the reverse Bénard–von Kármán wake (figure 3b), thus neutralizing the deflection of the propulsive jet which has been widely reported in the literature. The latter result, which is a novel observation, provides yet more evidence that wing compliance needs to be considered as a key parameter in the design of future flapping-propelled vehicles: not only does it determine thrust and efficiency but also, as we show here, it plays a role in dictating the vortex dynamics governing the stability properties of the wake.

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REFERENCES


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