

# Simple phalanx pattern leads to energy saving in cohesive fish schooling

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The question of how individuals in a population organize when living in groups arises for systems as different as a swarm of microorganisms or a flock of seagulls. The different patterns for moving collectively involve a wide spectrum of reasons, such as evading predators or optimizing food prospection. Also, the schooling pattern has often been associated with an advantage in terms of energy consumption. In this study, we use a popular aquarium fish, the red nose tetra fish, *Hemigrammus bleheri*, which is known to swim in highly cohesive groups, to analyze the schooling dynamics. In our experiments, fish swim in a shallow-water tunnel with controlled velocity, and stereoscopic video recordings are used to track the 3D positions of each individual in a school, as well as their tail-beating kinematics. Challenging the widespread idea of fish favoring a diamond pattern to swim more efficiently [Weihs D (1973) *Nature* 241:290–291], we observe that when fish are forced to swim fast—well above their free-swimming typical velocity, and hence in a situation where efficient swimming would be favored—the most frequent configuration is the “phalanx” or “soldier” formation, with all individuals swimming side by side. We explain this observation by considering the advantages of tail-beating synchronization between neighbors, which we have also characterized. Most importantly, we show that schooling is advantageous as compared with swimming alone from an energy-efficiency perspective.

fish swimming | collective dynamics | pattern formation | synchronization | energy efficiency

The dynamics of animal groups is driven by many different factors, such as foraging, social life, or survival instinct against predators (1). The collective movements are built from local interactions between the individuals constituting the group (2, 3). Apart from behavioral aspects, the benefit from schooling has often been associated with group optimization in terms of hydrodynamic resistance (4). A fish school represents a typical case of such cohesive and collaborative complex systems. The fluid dynamical mechanisms influencing the motion of fish in a school have been described in essence in the early study of Weihs (5). He demonstrated, using a 2D model, that if each fish maintains a specific position within the school, forming a diamond pattern, the hydrodynamic interactions will globally improve the swimming performance. The basic idea is that fish in a school optimize swimming by interacting constructively with the vortices shed by the local leading individuals; such constructive interactions require a precise synchronization between fish. This study has been followed by an extensive number of studies modeling or simulating fish school swimming configurations to validate Weihs’ hypothesis (6–8). It has been shown that by following this strategy, fish could improve their efficiency by ~20% (8, 9). However, the idea that a beneficial situation in terms of swimming power can be achieved for the group by maintaining a specific complex pattern remains, in some sense, a pure view from hydrodynamicists rather than an observation from nature. One of the shortcomings of the diamond pattern as a true descrip-

tion of natural systems lies in the strict 2D approach, which limits the comparison with real fish schools. There have certainly been several 3D computational studies on a single fish swimming (9–14), but very few exploring the case of fish swimming in groups (7). Another limitation of the diamond pattern is that its effectiveness imposes the strong constraint of maintaining a precise position and a quasiperfect synchronized kinematics of the individuals within the group (7). To a certain extent, this interesting and elegant view of fish group dynamics may be too idealized for noisy and multiple-parameter-dependent real schools.

In the present study, we investigate the energy-saving mechanisms of a fish school using real fish in a controlled swimming experiment. We chose for this purpose to examine the case of the red nose tetra fish, *Hemigrammus bleheri*. This species is particularly cohesive (15), thus representing a characteristic system to analyze collaborating interactions. It has been used in a recent study focusing on the interactions of neighboring fish swimming in pairs and triads—which can be considered the elementary subsystems of a fish school—that reported remarkable collaborative swimming features motivated by energy saving (16). This study especially showed that tail-beat synchronization increases dramatically when fish are forced to swim fast (i.e., in more energy-demanding gaits). How the nearest-neighbor dynamics scales up when considering larger schools is the question that we address in this work, where we have analyzed groups of up to nine individuals swimming at different speeds. The experimental apparatus allowed to explore a wide range of swimming speeds, from less than one body length per second (BL/s), which

## Significance

Fish school structures are firstly based on social life or prey-predator interactions, but another idea has often been raised by hydrodynamicists, claiming that fish could take advantage of schooling behavior from a locomotion efficiency perspective. By using a controlled swimming experiment with real schools, the present work shows that fish swimming together effectively need a less demanding stroke rate to sustain high swimming velocities, using, however, a different collective strategy compared with the usually suggested diamond pattern predicted by vortex-based interactions. The observed strategy, simply consisting of synchronized side-by-side swimming with nearest neighbors, finally, appears to be a lot more convenient for reaching an energy-saving regime.

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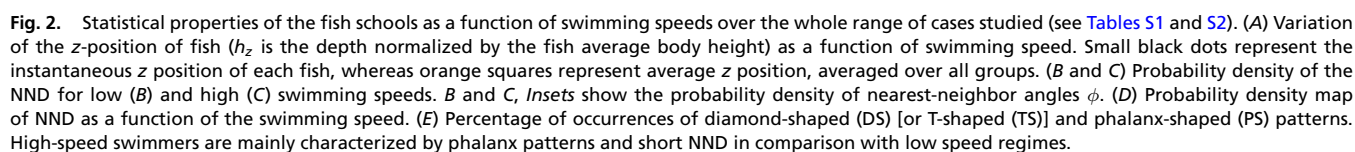
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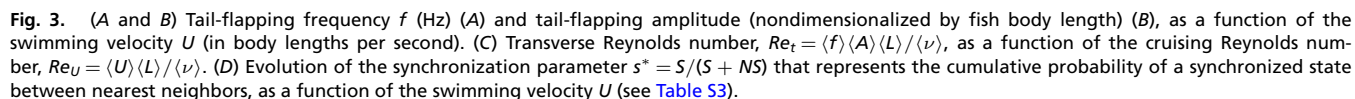
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fish behind the leading rows are placed between the two nearest neighbors in front of them), T-shaped (TS; where one fish follows directly behind one of the leaders), or in-line “phalanx-shaped” (PS; with fish swimming side by side and closer to each other) configurations (Fig. 2E). As can be noticed, PS configurations are dominant at high swimming velocity, independently of the school size.

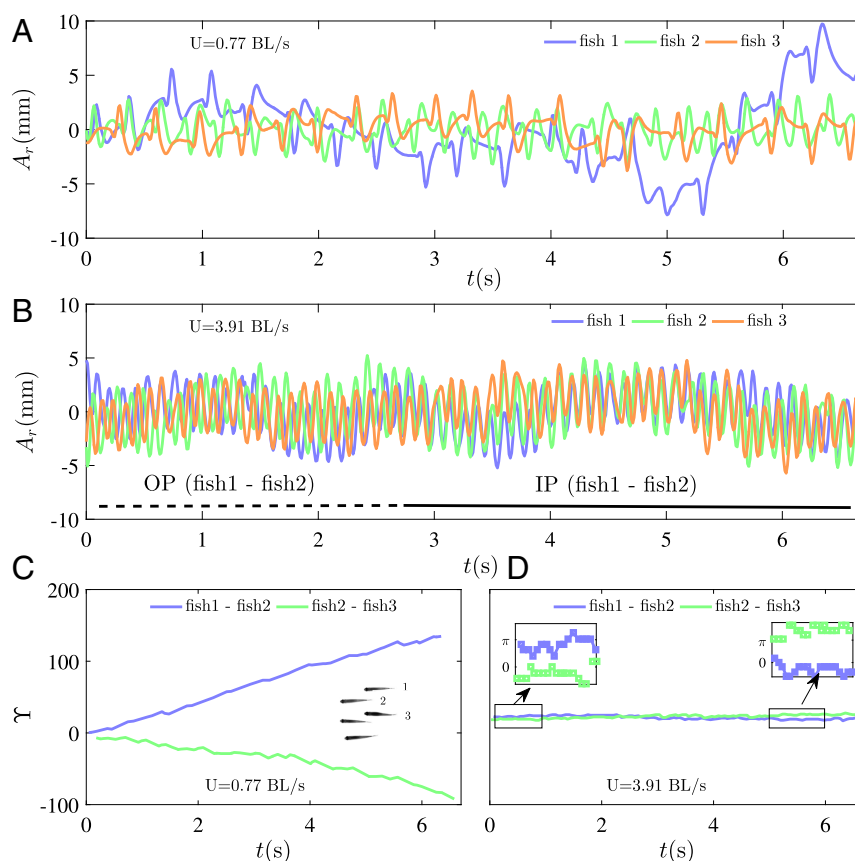
The central point now is to correlate the different spatial configurations of the schools with the observed tail-beating kinematics, which is how we probe the swimming efficiency of the school. Fig. 3 presents the kinematic measurements obtained from the midline tracking for all cases. The tail-beating frequency  $f$  and amplitude  $a$  are shown in Fig. 3 *A* and *B*, respectively, as a



function of the swimming velocity. As can be seen, no consequence of swimming in a group is observed on the tail-beating amplitude, which only increases slightly when fish are swimming faster. However, there is a clear effect on the frequency: Fish swimming alone use a higher frequency than those that have at least one neighbor. Moreover, this difference in tail-beating frequency increases with the swimming velocity. The frequency and amplitude observations can be summarized by using the dimensionless representation of Fig. 3C that shows the transverse Reynolds number  $Re_t = faL/\nu$  as a function of the usual cruising Reynolds number  $Re_U = UL/\nu$ . The  $Re_t$  has also been named the “swimming number” in a recent study on the scaling of macroscopic aquatic locomotion (22) and has been used in the literature to describe flapping-based locomotion (e.g., ref. 23). Because the amplitude is almost constant, the dimensionless  $Re_t$  vs.  $Re_U$  curve reproduces the results already described in the frequency curve. Another quantity usually used to describe animal swimming is the Strouhal number  $St = fa/U$  (e.g., ref. 24), which is related to swimming efficiency because it compares the input effort of the fish characterized by the flapping velocity  $fa$  to the output represented by the swimming velocity  $U$ . The values of  $St$  resulting from the present observations range between 0.3 and 1.5 (Fig. S1). In accordance with the observations for the frequency and amplitude, the average Strouhal numbers for fish schools are lower than those for fish swimming alone at the same velocities. Combining the observations on the school patterns and the beating kinematics, we note that the most frequent patterns corresponding to efficient swimming (i.e., low values of

Strouhal number) are characterized by a side-by-side phalanx configuration.

The other remarkable feature observed in the fish schools is the change of synchronization of tail-beating kinematics between neighboring individuals within a group. The time series of the caudal fin tip motion for three neighboring fish in a group of five are reported in Fig. 4, at low swimming velocity (close to the natural speed of free swimming; Fig. 4A) and high swimming velocity (representing a high-energy-demanding situation; Fig. 4B). Fish swimming together at their free-ranging speed do not show any sign of correlation in their respective kinematics; the phase differences in Fig. 4C,  $\Upsilon$  between one individual (fish 2) and its two nearest neighbors (fish 1 and 3), show a constant drift (almost linear) with time, typical of uncorrelated dynamics (25). Fast swimmers, on the contrary, show strong synchronized dynamics (Fig. 4B), characterized by in-phase (IP) and out-of-phase (OP) modes. In contrast to the low-speed regime, the synchronization is confirmed here by constant phase differences (25) all along the measurement time (Fig. 4D). The phase difference is calculated by a peak identification routine on each time series of the tail-beating amplitude. The synchronization effect for *H. bleheri* was already pointed out in a study with fish pairs (16), in which observations of a large set of experiments showed that  $>90\%$  of the fish pairs studied were synchronized when swimming at high speed. Fig. 3D presents the synchronization rate  $s^* = S/(S + NS)$  as a function of the swimming velocity, where  $S$  and  $NS$  are the total number of synchronized and nonsynchronized states, respectively. This demonstrates



**Fig. 4.** Examples of time series of the tail tip amplitude for one given individual (fish 2) within the school and its two nearest neighbors (fish 1 and 3). (A and B) Low (A) and high (B) swimming speed. The in-phase (IP) and out-of-phase (OP) swimming regimes are also shown. (C and D) Evolution of the phase difference  $\Upsilon$  between fish 2 and its two nearest neighbors (fish 1 and 3) showing a nonsynchronized state (NS) at low swimming speed (C) and strongly synchronized state (S) at high swimming speeds (D). D, Insets show zooms in the case of synchronized swimming that are either around 0 (for IP synchronization) or  $\pi$  (for OP synchronization).



that high synchronization is a general behavior in schools sustaining high swimming gaits. It also supports the idea of considering local interactions within a subgroup of nearest neighbors as the minimal unit to describe the dynamics of larger schools.

## Discussion

We have shown that schools of the cohesive fish species *H. bleheri* sustaining a high swimming speed gather in a phalanx configuration, rather than in the diamond pattern described as the most efficient by a 2D hydrodynamics idealized view. These phalanx configurations actually appear to be efficient, if one measures the advantage of schooling by the net decrease in the tail-beating frequency observed for fish swimming in a group, when compared with the case of a single fish swimming alone (Fig. 3). The tail-beat frequency is directly correlated with the oxygen consumption rate of the fish—oxygen consumption being an indirect measure of metabolic rate and energy consumption (26–34). Therefore, the decrease in tail-beat frequency can be considered as a decrease in energy consumption. Indeed, while at low velocities, the benefit is barely observable, it is significant at the more energy-demanding, higher-velocity regimes, where almost all schooling occurs in phalanx formation. Moreover, the occurrence of the phalanx formation is correlated with the observation of local kinematic synchronization of each swimmer with its nearest neighbors.

Several arguments can be put forward to understand the formation of an efficient pattern in the *H. bleheri* schools studied here. Swimming in a packed side-by-side phalanx configuration has been identified by 2D and 3D simulations as a good strategy to optimize thrust or efficiency by using channeling effects, especially at small clearance ( $\sim 0.5$  BL) and IP synchronized kinematics of nearest neighbors (7, 8, 35). In particular, Hemelrijk et al. (8) confirmed the advantage of PS and DS configurations over solitary swimming in terms of Froude efficiency. Daghooghi and Borazjani (7) underlined, based in full 3D simulations, that the wakes shed by the swimmers show strong differences with the 2D idealized view at the core of Weihs' description of the diamond pattern (5). They reported that the primary vortices shed by the fish tail break down rapidly into smaller vortices, leading to a rather disorganized wake structure with very low chance for constructive vortex interaction. In the phalanx configuration, on the other hand, the case of OP synchronization between neighbors—which has already been noted to be slightly preferred to IP synchronization in previous experiments with fish pairs (16)—can be expected to be beneficial in terms of propulsive performance owing to the jet-like profile produced by two neighboring fish. The latter mechanism has been demonstrated in the literature by using numerical simulations (36) and experiments with model swimmers (37). In summary, synchronization either IP or OP should give an advantage to fish swimming in groups, especially when nearest neighbors come closer to each other. The prevalence of phalanx configurations at high swimming velocities observed in the present experiments, together with their correlation to a high rate of kinematic synchronization between nearest neighbors, confirms that these physical mechanisms are indeed at play in a real fish school.

Additionally, as evoked above, the possibility of taking advantage of a diamond pattern might be uncertain for actual swimming animals: Fish must maintain a perfectly ordered configuration. These issues were already remarked on by Weihs (5) and have been the center of criticisms in previous studies (19, 38, 39), because achieving the required conditions to maintain such idealized diamond patterns may be too constraining for a school. Choosing a phalanx pattern appears to be the selected strategy to

optimize swimming performance, combining social and mechanical priorities together. It remains to be confirmed if the conclusions reached here for *H. bleheri* is valid for other species and other experimental conditions.

## Materials and Methods

**Animals and Housing.** Red nose tetra fish, *H. bleheri*, of body length in the range  $\sim 3.5$ – $4$  cm long and height  $\sim 0.5$ – $0.6$  cm, were procured from a local aquarium supplier (anthias.fr). The fish were reared in a 60-L aquarium tank with water at a temperature between 26 and 27 °C, and they were fed five to six times a week with commercial flake food. The experiments performed in this study were conducted under the authorization of the Buffon Ethical Committee (registered to the French National Ethical Committee for Animal Experiments no. 40).

**Flow Characterization in the Water Tunnel.** A shallow-water tunnel with a test section of 2.2 cm depth and a swimming area of 20 cm  $\times$  15 cm (Fig. S2) was used for the experiments. The flow rate  $Q$  could be varied from 4 to 22 L per minute, resulting in an average velocity  $U = Q/S$ , where  $S$  is the cross-section, in the range between 2.7 cm  $\cdot$  s $^{-1}$  to 15 cm  $\cdot$  s $^{-1}$ . To characterize the flow in the channel, particle image velocimetry measurements were carried out in the midplane of the channel. The mean turbulence intensity (TI) was found to be between 3 and 5% and it seemed to be independent of the flow rate (Fig. S3A). Fig. S3B shows the velocity profile in the midsection of the channel, which also remained unchanged for the different flow rates. We note also that the velocity profile was rather flat, with the wall effect region being limited to a distance  $< 3$  mm. The minimum distance between the fish and the wall was, in the most confined case (the nontet case),  $\approx 7$  times the size of the wall effect region. This distance was  $> 14$  times the size of the wall effect region for the other groups. The wall effect is therefore negligible.

**Experimental Procedure.** Before starting each run, the fish were transferred with a hand net from the rearing tank to the test section of the channel without any flow. The fish were left idle for  $\sim 1$  h in the channel without any flow to get habituated to the shallow test section. Each of the swimming tests was carried out for 10 s. After each test with a fish group, the fish were allowed to relax for  $> 20$ – $30$  min in the channel without flow. After a complete set of experiments (consisting typically of 10 tests at 10 different velocities), each group was transferred to another tank. No individual fish has participated in any other group.

**Visualization.** The fish kinematics were recovered from top-view visualizations at 100 frames per second. An in-house code, written in Matlab, was used to track the fish and extract boundary points and midline kinematics from the movies. For each image, the background was subtracted from the image to get the silhouette. Then, the processed image was binarized by using Otsu's method (40). The boundary points on each side of the fish and the head were identified for each fish. Finally, we obtained the midline, equidistant from the lateral boundaries of each fish. Thus, we obtained for each fish its full spatiotemporal evolution. For 3D tracking, we modified the 3D tracking software by Hedrick (41) and made it automated to meet our requirements. Images from two side cameras were taken. The centroid of each fish eye was then tracked from the binarized image. The 3D reconstruction was then carried out by using direct linear transformation, which converted 2D camera-space coordinates into 3D global coordinates.

**Data Statistics.** The tail-beating kinematics was extracted for each fish in a group. The average and SD were computed for each group and each velocity. All points presented in Fig. 3 are thus averaged quantities with several experiments per point. For instance, the data points for the frequency are given by  $f = \frac{1}{N} \sum_0^N (f)$  over the number of individuals and the different runs, where the brackets denote a time average and  $N$  is the number of individuals within the school. Thus, we obtained a single value of the frequency for each group size and swimming speed.

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# Supporting Information

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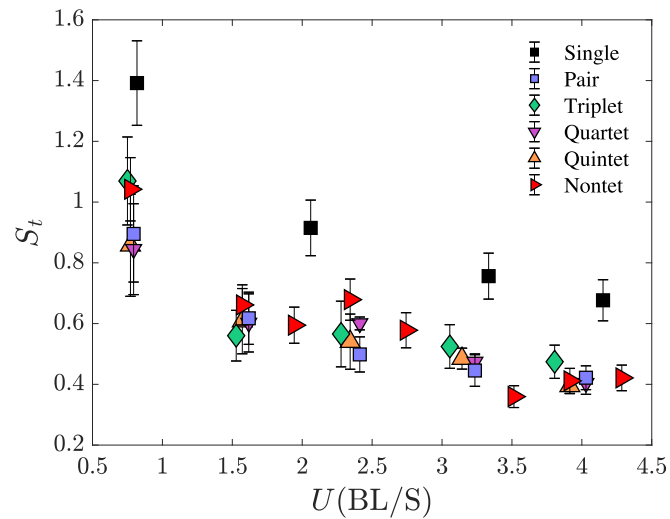


Fig. S1. Strouhal number as a function of the swimming velocity.

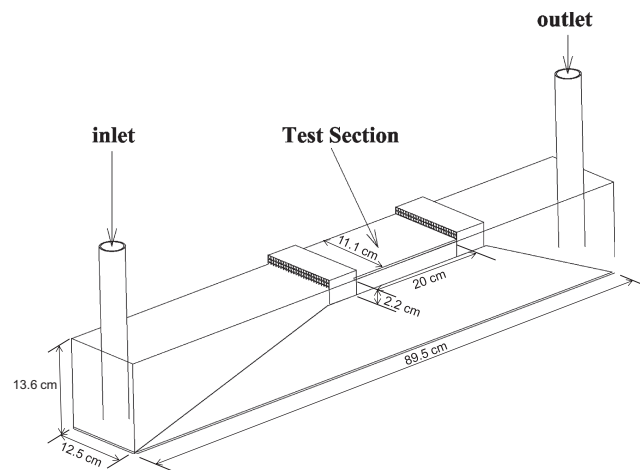


Fig. S2. Schematic diagram of the swimming channel. An external pump drives the flow, which is directed toward the test section after a convergent ramp and through a honeycomb section to minimize swirling motions. A second honeycomb delimits the test section downstream.

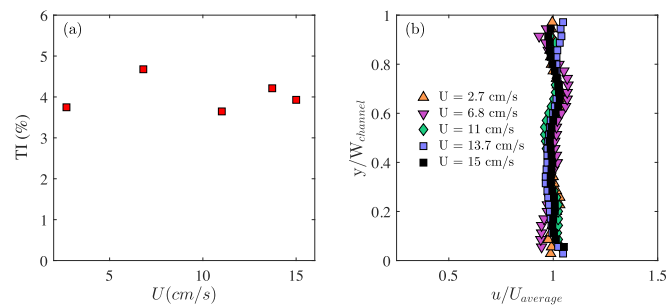


Fig. S3. (A) Turbulence intensity (TI) as a function of the average flow velocity in the channel. It can be seen that the turbulence in the flow remains fairly constant over the flow rate range explored and remains at  $<5\%$ . (B) The velocity profile in the  $x$  direction at midheight and midsection of the channel,  $u(y)$ , is rather flat and also does not change with the flow rate.

**Table S1. Numbers of experiments for 3D tracking (Fig. 2 A–D)**

Experiment type	0.77 BL/s	1.17 BL/s	1.57 BL/s	1.94 BL/s	2.34 BL/s	2.74 BL/s	3.14 BL/s	3.51 BL/s	4.0 BL/s	4.2 BL/s
Nontet	2	1	3	2		2		2	2	
Quintet	4	6	4	4	4	4	7	3	5	3
Quartet	11	11	8	5	7	7	8	6	7	3
Triplet	10	8	10	11	12	9	4	9	5	7

**Table S2. Numbers of experiments for Fig. 2E**

	0.77	1.17	1.57	1.94	2.34	2.74	3.14	3.51	4.0	4.2
Experiment type	BL/s	BL/s	BL/s	BL/s	BL/s	BL/s	BL/s	BL/s	BL/s	BL/s
Nontet	5	5	4	6	5	6	6	6	6	6
Quintet	19	19	18	18	17	20	19	18	18	12
Quartet	33	29	23	21	26	22	23	21	23	13
Triplet	27	18	18	28	18	18	28	18	28	18

Table S3. Numbers of experiments for Fig. 3

Experiment type	0.77 BL/s	1.17 BL/s	1.57 BL/s	1.94 BL/s	2.34 BL/s	2.74 BL/s	3.14 BL/s	3.51 BL/s	4.0 BL/s	4.2 BL/s
Nontet	2	1	3	2		2		2	2	2
Quintet	8		4		4		4		4	
Quartet	5		4		5		5		6	
Triplet	5		5		5		5		5	
Pair	8		8		8		8		8	
Single	1		1		1		1		1	



**Movie S1.** Four fish swimming at 0.77 BL/s.

[Movie S1](#)





**Movie S2.** Nine fish swimming at 0.77 BL/s.

[Movie S2](#)



**Movie S3.** Four fish swimming at 3.91 BL/s.

[Movie S3](#)



**Movie S4.** Nine fish swimming at 3.91 BL/s.

[Movie S4](#)