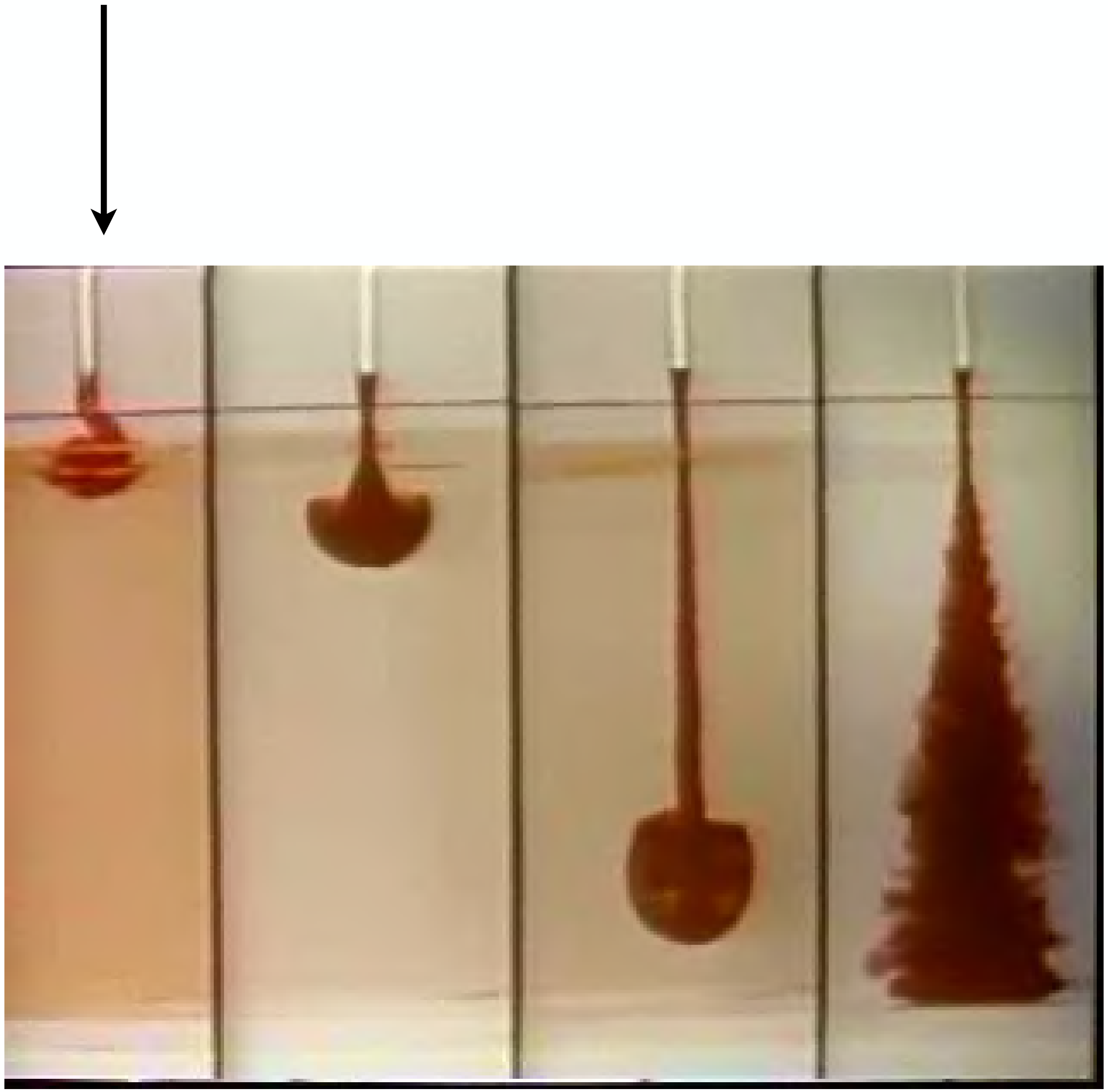
Un monde sans inertie



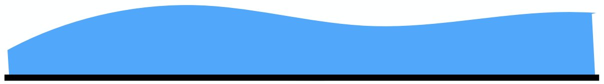
Les écoulements à petit nombre de Reynolds

Pas d'inertie

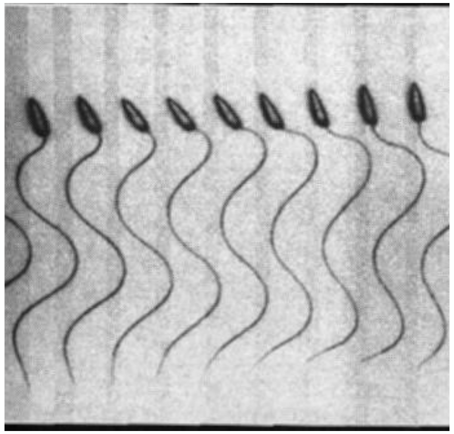
Navier-Stokes → Équation de Stokes

$$\eta \Delta \mathbf{u} = \nabla p$$

Les écoulements en couche mince et l'approximation de lubrification

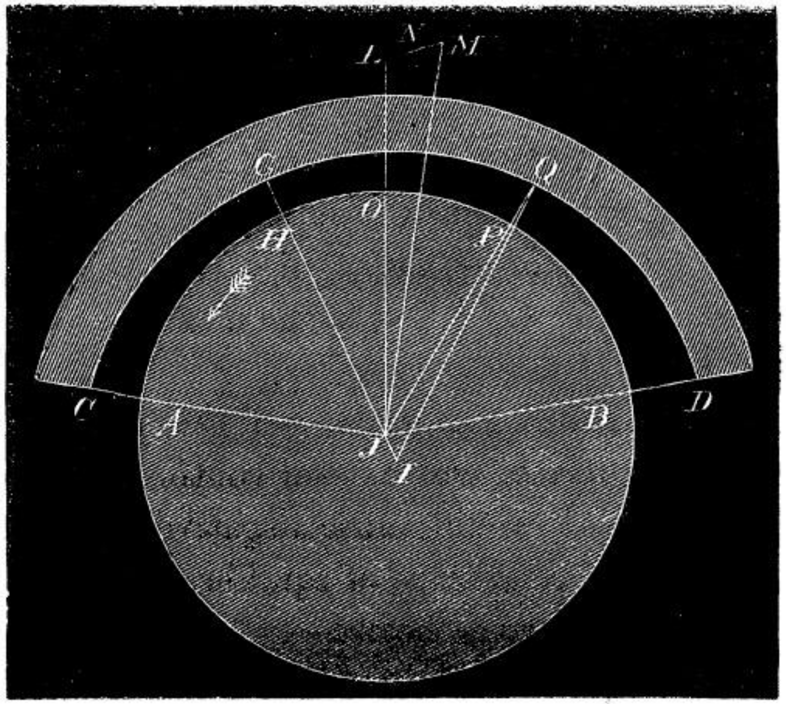


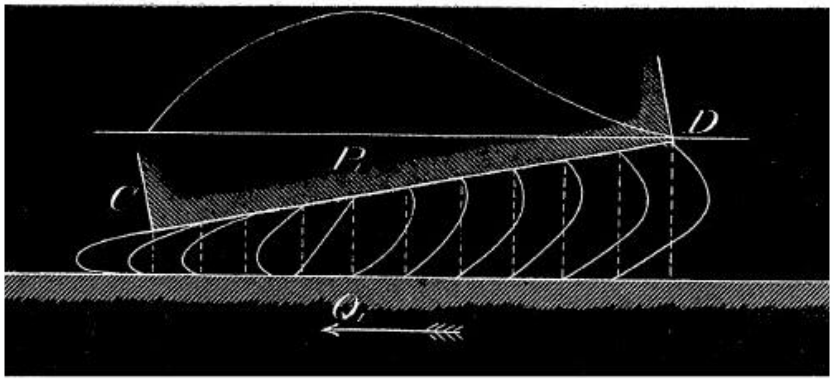
Les forces sur les objets solides, la réversibilité cinématique et la propulsion à petit Reynolds



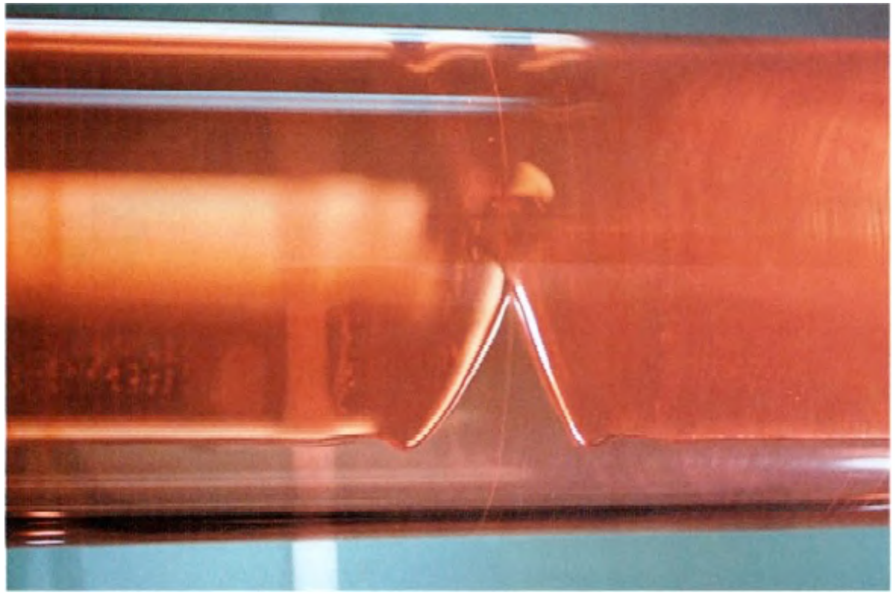
Les écoulements visqueux en couches minces

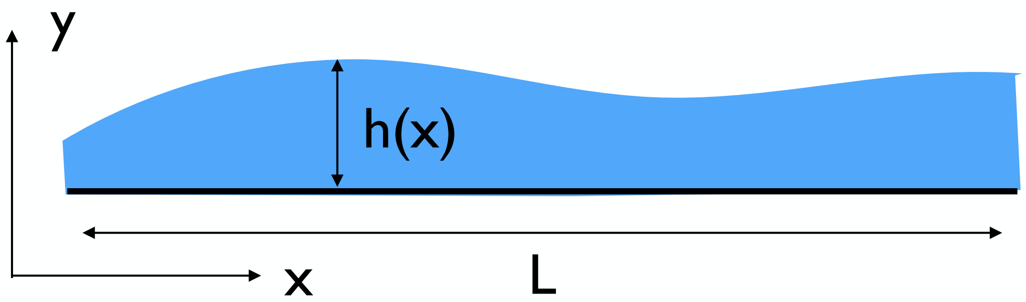
Lubrification (Reynolds 1882)





Écoulements en couche mince à surface libre

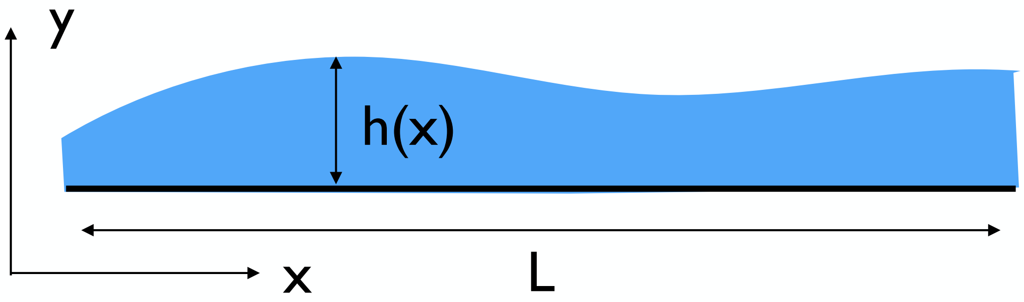




$$h \ll L$$

$$\nabla . \mathbf{u} = \frac{\partial u_x}{\partial x} + \frac{\partial u_y}{\partial y} \sim \frac{u_x}{L} + \frac{u_y}{h}$$

$$\frac{u_x}{u_y} \sim \frac{L}{h} \gg 1$$



$$\frac{u_x}{u_y} \sim \frac{L}{h} \gg 1$$

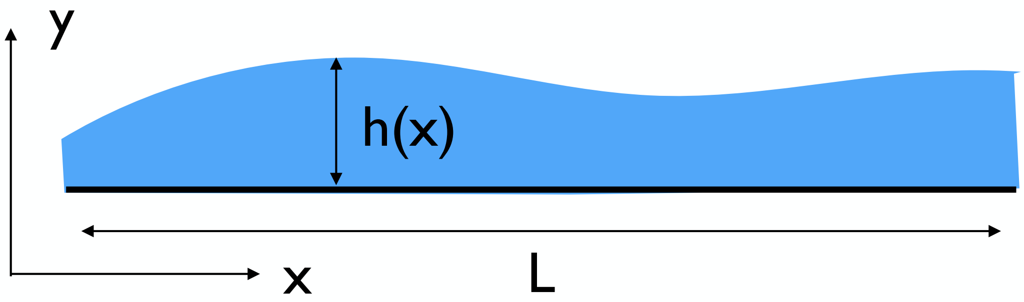
$$0 = -\frac{\partial p}{\partial x} + \eta \left(\frac{\partial^2 u_x}{\partial x^2} + \frac{\partial^2 u_x}{\partial y^2} \right)$$

$$\frac{\partial p}{\partial x} = \eta \frac{\partial^2 u_x}{\partial y^2}$$

$$\frac{U}{L^2} \qquad \frac{U}{h^2}$$

$$0 = -\frac{\partial p}{\partial y} + \eta \left(\frac{\partial^2 u_y}{\partial x^2} + \frac{\partial^2 u_y}{\partial y^2} \right)$$

$$\frac{\partial p}{\partial y} \sim 0$$



$$\frac{\partial p}{\partial x} = \eta \frac{\partial^2 u_x}{\partial y^2} \qquad \frac{p}{L} \sim \eta \frac{U}{h^2} \qquad F_y \sim pL \sim \eta U \frac{L^2}{h^2}$$

$$\sigma_{xy} = \eta \frac{\partial u_x}{\partial y} \sim \eta \frac{U}{h} \qquad F_x \sim \sigma_{xy} L \sim \eta U \frac{L}{h}$$

$$\boxed{\frac{F_y}{F_x} \sim \frac{L}{h} \gg 1}$$