Brittle fracture under mode I+III loading

veronique.lazarus@ensta.fr Prof ENSTA ParisTech/UME IMSIA (CNRS, CEA, EdF, ENSTA), Palaiseau



Lazarus, Buchholz, Fulland, Wiebesiek, IJF 2008

A glimpse on the complexity of the propagation in presence of mode III...

Modes



- Mode I: opening
- ► Mode II: shearing
- Mode III: tearing

Outline

Experimental observations

Mode I+II Mode I+III

Linear Elastic Fracture Mechanics (LEFM)

Is LEFM able to predict the experimental observations? Mode I+II Mode I+III

Mode I+II



The crack doesn't extend in its plane,

but kinks to reach a mode I orientation.

Mode I



Chap. 'Endommagement, rupture', Lazarus (La matière en désordre, EDP, 2014

The path is nearly straight.

Mode I: From straight to more complex paths Yuse et Sano, 1993, 1997; Ronsin et al., 1995; Yang and Ravi-Chandar, 2001



Fig. 1. Temperature configuration of the experiment. A thin sample plate moves slowly across the temperature gradient gap in the direction of the arrow with velocity V.

From Yuse et Sano, 1993, 1997

Though the crack is initially loaded in mode I, out of plane propagation may occur.

Mode I+III . Pioneer experiments.

Segmentation and *progressive* rotation of the facets



Sommer (1969)

Nucleation of *abrupt* rotated facets



Knauss (1970)

Mode I+III. 3 point bending experiments (Macroscale)





Buchholz et al. (2004); Lazarus et al. (2008)

At the macroscale, the front twists due to the presence of mode II...

Mode I+III. 3 point bending experiments (Microscale)



Chen et al. (2015)

- 1. Apparition of small tilted finger shaped facets
- 2. Progressive coalescence
- 3. Facets are rotated toward the shear-free direction

Similar observations in other materials, e.g. Lin et al. (2010), and setups...

Mode I+III. An experiment on cheese



Goldstein and Osipenko (2012)

Mode I+III. Transition smooth/facets

► Ronsin et al. (2014)



Fig. 1: (Colour on-line) Skotch of the experimental setup: the gol slab (unstrained dimension $L \times h \times c$), once stretched by Δh_1 is notelised at angle θ_1 by the black B.



 $\theta_0 < \theta_0^c$ and $\theta_0 > \theta_0^c$

► Eberlein et al. (2017)



In these experiments, the precrack is a 'real' *sharp* crack. 11/36

Mode I+III. Facets whatever the amount of mode III Pham and Ravi-Chandar (2014)



In these experiments, the precrack is not sharp.

Mode I+III. Focus on the initiation of the facets

Pham and Ravi-Chandar (2016)



- Facets are rotated toward the shear-free direction
- The initial spacing between the facets dictated by the thickness of the initial crack.

Mode I+III. Main experimental observations



- 2 regimes depending on the amount of mode III:
 - 1. smooth propagation
 - 2. fragmentation of the initial crack into facets

What governs the transition?

- Facets morphology :
 - 1. Apparition of small tilted finger shaped facets
 - 2. Progressive coalescence
 - 3. Facets are rotated toward the shear-free direction

Is it possible to predict their shape qualitatively... quantitatively?

Outline

Experimental observations Mode I+II Mode I+III

Linear Elastic Fracture Mechanics (LEFM)

Is LEFM able to predict the experimental observations? Mode I+II Mode I+III

LEFM. Framework



Local loading is given by:

- Stress Intensity Factors: $K_{I}(s), K_{II}(s), K_{III}(s)$.
- ► Energy release rate *G*:

$$\mathcal{G}(s) \equiv -\frac{dE_{elast}}{dS} = \frac{1-\nu^2}{E}(K_l(s)^2 + K_{ll}(s)^2) + \frac{1+\nu}{E}K_{lll}(s)^2$$

Irwin's formula

LEFM. Propagation criteria



Suitable to predict the propagation of each point of the front...

LEFM. Nucleation of abruptly twisted facets

...but not for the nucleation of abruptly twisted facets.



Direction of the maximum principal stress axis

$$\tan 2\theta = \frac{K_{III}/K_I}{\frac{1}{2}-\nu}$$

Cooke and Pollard (1996)

Outline

Experimental observations Mode I+II Mode I+III

Linear Elastic Fracture Mechanics (LEFM)

Is LEFM able to predict the experimental observations? Mode I+II Mode I+III

Mode I+II. Propagation direction

PLS is verified experimentally



Erdogan and Sih (1963); Flores and Xu (2013)

Mode I: From straight to more complex paths Yuse and Sano, 1993, 1997; Ronsin et al., 1995; Yang and Ravi-Chandar, 2001



Yuse and Sano (1993)

If $V > V_c$ or $\Delta T > \Delta T_c$, the path is no more straight

Mode I: Bifurcation from straight to wavy paths

• The straight propagation is not the unique solution of $K_{II} = 0$.



Video on Blaise Bourdin webpage. Bourdin et al. (2008)

Supercritical bifurcation



Corson et al. (2009)

Mode I+III: a thought experiment



Uniform loading:

 $egin{aligned} & K_{I}(s) = K_{I} \ & K_{II} = 0 \ & K_{III}(s) = K_{III} \end{aligned}$

Planar crack with straight front in an infinite and homogeneous media

Straight uniform propagation is a trivial solution of $G = G_c$ and $K_{II} = 0$

But neither unique, nor stable...

Mode I+III: Helical crack front bifurcation





Pons and Karma (2010)

Mode I+III: Linear stability analysis

Leblond, Karma, Lazarus (JMPS, 2011)



For
$$K_{III}/K_I > (K_{III}/K_I)_c(\nu)$$
,

the straight propagation is unstable versus wavy out+in-plane perturbations of all wavelength.

$$\delta G = \delta G)_{in-plane} + \delta G)_{out-plane} = 0$$

$$\delta K_{II} = \delta K_{II})_{in-plane} + \delta K_{II})_{out-plane} = 0$$

Gao and Rice (1986) Movchan et al. (1998)

Mode I+III: Non linear analysis

Above the threshold: Karma and Pons (Nature, 2010)



The propagation is unstable in agreement with linear stability analysis.

Below the threshold:

Chen, Cambonie, Lazarus, Nicoli, Pons, Karma (PRL, 2015)



1. Starting from a 'perfectly' straight crack,

no instability appears;

- 2. The instability can be initiated by decreasing K_{III}/K_I from above to below the threshold.
 - The instability is subcritical and may be initiated by small imperfections (confirmed by Henry (2016))

Mode I+III: subcritical bifurcation/experiments

Subcritical bifurcation implies that the transition is sensitive to defects, and that:

▶ it may be observed...



Ronsin et al. (2014); Eberlein et al. (2017)

or not:



Pham and Ravi-Chandar (2014)

Facets morphology at initiation

Pham and Ravi-Chandar (2016)



Facets are rotated in the shear-free direction given by

$$\tan 2\theta = \frac{K_{III}/K_I}{\frac{1}{2}-\nu}$$

The spacing between the facets dictated by the thickness of the initial crack.

Further propagation

Qualitative agreement between experiments and phase-field simulations.

Chen, Cambonie, Lazarus, Nicoli, Pons, Karma (PRL, 2015)



- After initiation, the facets take some finger shape;
- They further coalesce
- The rotation angle is nearly constant

And quantitatively?

Quantitative description of the crack profile

Cambonie and Lazarus (Procedia Materials Science, 2014)

1. Mechanical profilometer to get a mapping of the fracture surface



2. We extract:

the facet rotation angle θ the coarsening rate $\beta \equiv \frac{d\lambda}{da}$.

Facet rotation angle. Phase-field/experiments



- quantitative agreement for θ between experiments and PF;
- shear-free orientation overestimates the angle θ .
- discrepancy with Pham and Ravi-Chandar (2016) at initiation

Additional experiments are necessary to conclude. Interaction between cracks may play a role (Leblond and Frelat, 2014)?

Coarsening rate



- β increases with K_{III}/K_I
- Agreement via an adjustable parameter,

...additional work is necessary.

Conclusion on facets morphology



Apparition of small tilted finger shaped facets

- 2. Facets are rotated toward the shear-free direction
- 3. Progressive coalescence

LEFM is able to predict the morphology

TODO:

- What determines β ?
- Focus on the initiation (initial distance and angle evolution, smooth/abrupt). LEFM limit?

Conclusion on the smooth/facets transition

A subcritical bifurcation has been evidenced by non-linear stability analysis, explaining why a transition may be observed or not.



Eberlein et al. (2017)

TODO: understand the role of the defects on the onset of the instability?

It may be necessary to focus below the scale of LEFM...

On going work in the LEFM framework

Study

the morphology

the impact of facets on the propagation (toughness, velocity) with the use of:

- Additional phase-field simulations
- Additional experiments (3 PB, multiaxial testing machine)
- Multiscale approach:

Macroscopic view: facets appear as a cohesive zone



Microscopic view: facets appear as echelon cracks



Leblond, Lazarus, Karma (IJF, 2015)

That's it for today! Thanks to co-workers and for your attention... Questions?

References

- Bourdin, B., Francfort, G., Marigo, J.-J., 2008. The variational approach to fracture. Journal of elasticity 91 (1), 5 148.
- Buchholz, F.-G., Chergui, A., Richard, H. A., 2004. Fracture analyses and experimental results of crack growth under general mixed mode loading conditions. Engineering Fracture Mechanics 71 (4-6), 455–468.
- Cambonie, T., Lazarus, V., 2014. Quantification of the crack fragmentation resulting from mode I+III loading. Procedia Materials Science 3, 1816–1821.
- Chen, C.-H., Cambonie, T., Lazarus, V., Nicoli, M., Pons, A. J., Karma, A., 2015. Crack Front Segmentation and Facet Coarsening in Mixed-Mode Fracture. Physical Review Letters 115 (26), 265503.
- Cooke, M. L., Pollard, D. D., 1996. Fracture propagation paths under mixed mode loading within rectangular blocks of polymethyl methacrylate. Journal of Geophysical Research 101 (B2), 3387–3400.
- Corson, F., Adda-Bedia, M., Henry, H., Katzav, E., 2009. Thermal fracture as a framework for quasi-static crack propagation. International Journal of Fracture 158 (1), 1–14.
- Eberlein, A., Richard, H., Kullmer, G., 2017. Facet formation at the crack front under combined crack opening and anti-plane shear loading. Engineering Fracture Mechanics 174, 21 – 29, special Issue on Multiaxial Fracture 2016.

URL http://www.sciencedirect.com/science/article/pii/S0013794416307354

- Erdogan, G., Sih, G. C., 1963. On the crack extension in plates under plane loading and transverse shear. ASME J. Basic Engng 85, 519–527.
- Flores, M., Xu, L. R., Oct. 2013. An efficient mixed-mode brittle fracture experiment using paper. International Journal of Fracture 183 (2), 267–273.
- Goldstein, R., Osipenko, N., 2012. Successive development of the structure of a fracture near the front of a longitudinal shear crack. Doklady Physics 57, 281–284, 10.1134/S1028335812070087.

URL http://dx.doi.org/10.1134/S1028335812070087

- Goldstein, R. V., Salganik, R. L., 1974. Brittle fracture of solids with arbitrary cracks. International Journal of Fracture 10, 507–523.
- Griffith, A. A., 1920. The phenomena of rupture and flow in solids. Philosophical Transactions of the Royal Society of London 221, 163–198.
- Henry, H., 2016. Crack front instabilities under mixed mode loading in three dimensions. EPL (Europhysics Letters) 114 (6), 66001.
- Knauss, W. G., Jun. 1970. An observation of crack propagation in anti-plane shear. International Journal of Fracture Mechanics 6 (2), 183–187.

URL http://link.springer.com/article/10.1007/BF00189825

- Lazarus, V., Buchholz, F.-G., Fulland, M., Wiebesiek, J., 2008. Comparison of predictions by mode II or mode III criteria on crack front twisting in three or four point bending experiments. International Journal of Fracture 153, 141–151.
- Leblond, J., Karma, A., Lazarus, V., 2011. Theoretical analysis of crack front instability in mode I+III. Journal of the mechanics and physics of solides 59, 1872–1887.
- Leblond, J.-B., Frelat, J., 2014. Development of fracture facets from a crack loaded in mode I+III: solution and application of a model 2D problem. Journal of the Mechanics and Physics of Solids 64, 133–153.

URL http://www.sciencedirect.com/science/article/pii/S002250961300224X

- Leblond, J.-B., Lazarus, V., Karma, A., February 2015. Multiscale cohesive zone model for propagation of segmented crack fronts in mode I+III fracture. International Journal of Fracture (Special Invited Article Celebrating IJF at 50) 191 (1), 167–189.
- Lin, B., Mear, M., Ravi-Chandar, K., 2010. Criterion for initiation of cracks under mixed-mode i + III loading. International Journal of Fracture 165, 175–188, 10.1007/s10704-010-9476-7.
- Pham, K. H., Ravi-Chandar, K., Oct. 2014. Further examination of the criterion for crack initiation under mixed-mode i+III loading. International Journal of Fracture 189 (2), 121–138.
- Pham, K. H., Ravi-Chandar, K., Mar. 2016. On the growth of cracks under mixed-mode I + III loading. International Journal of Fracture , 1-30