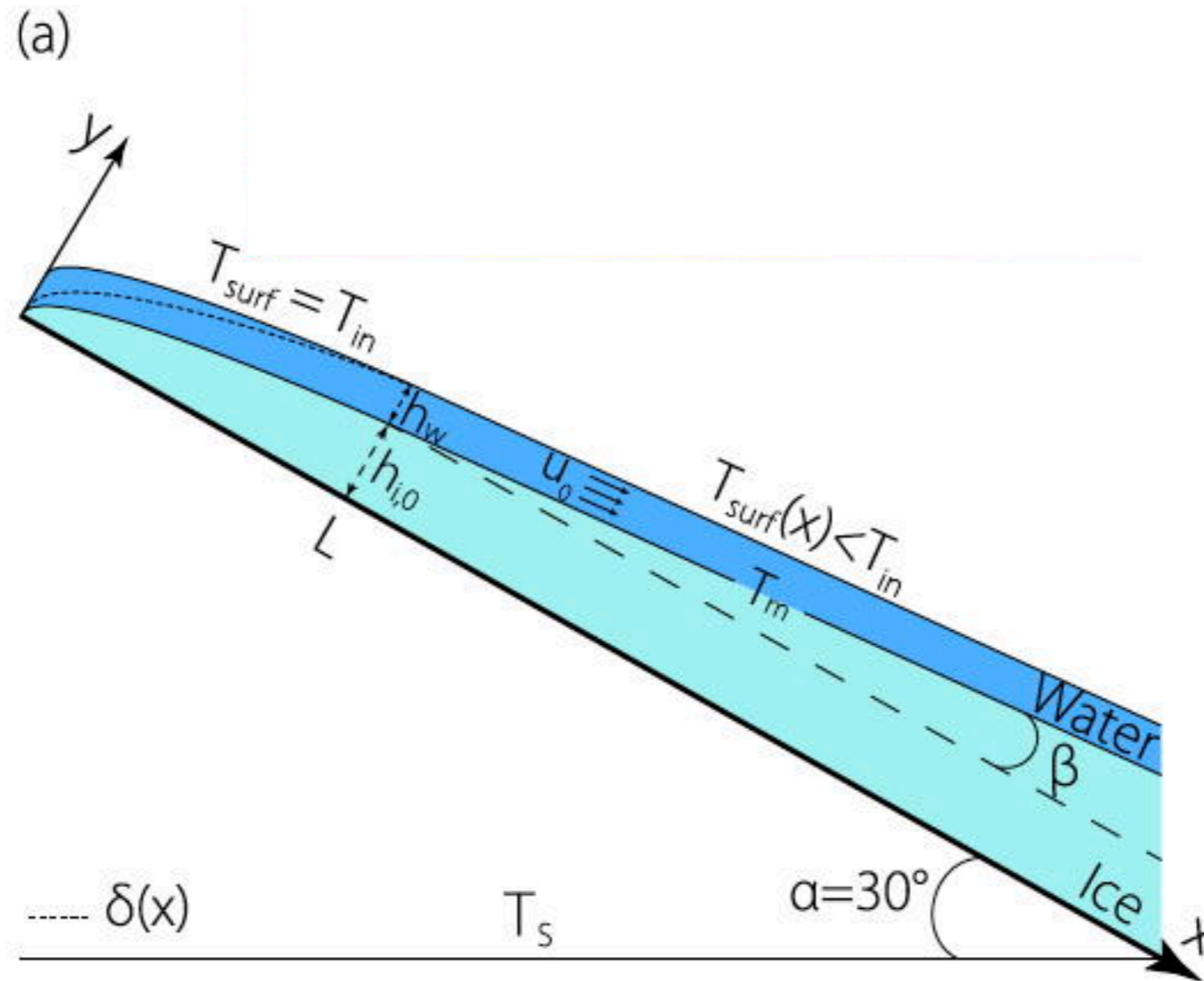
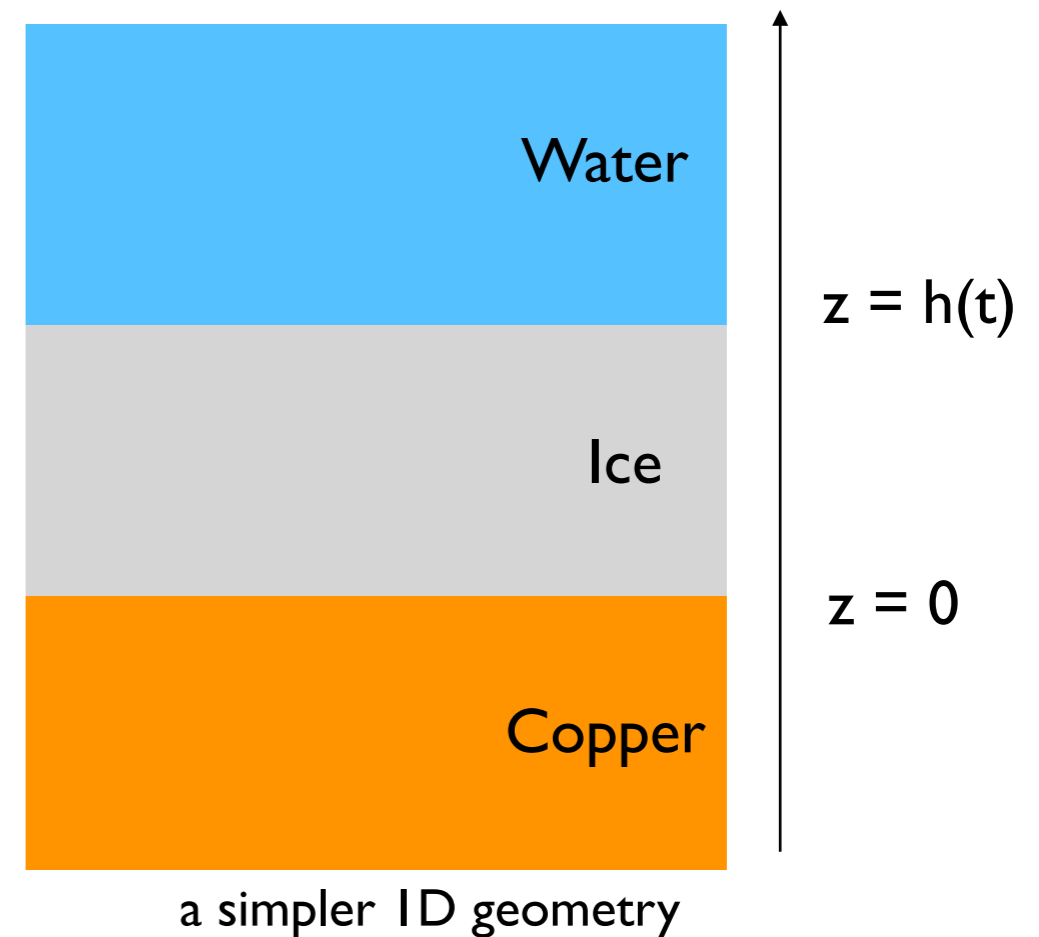
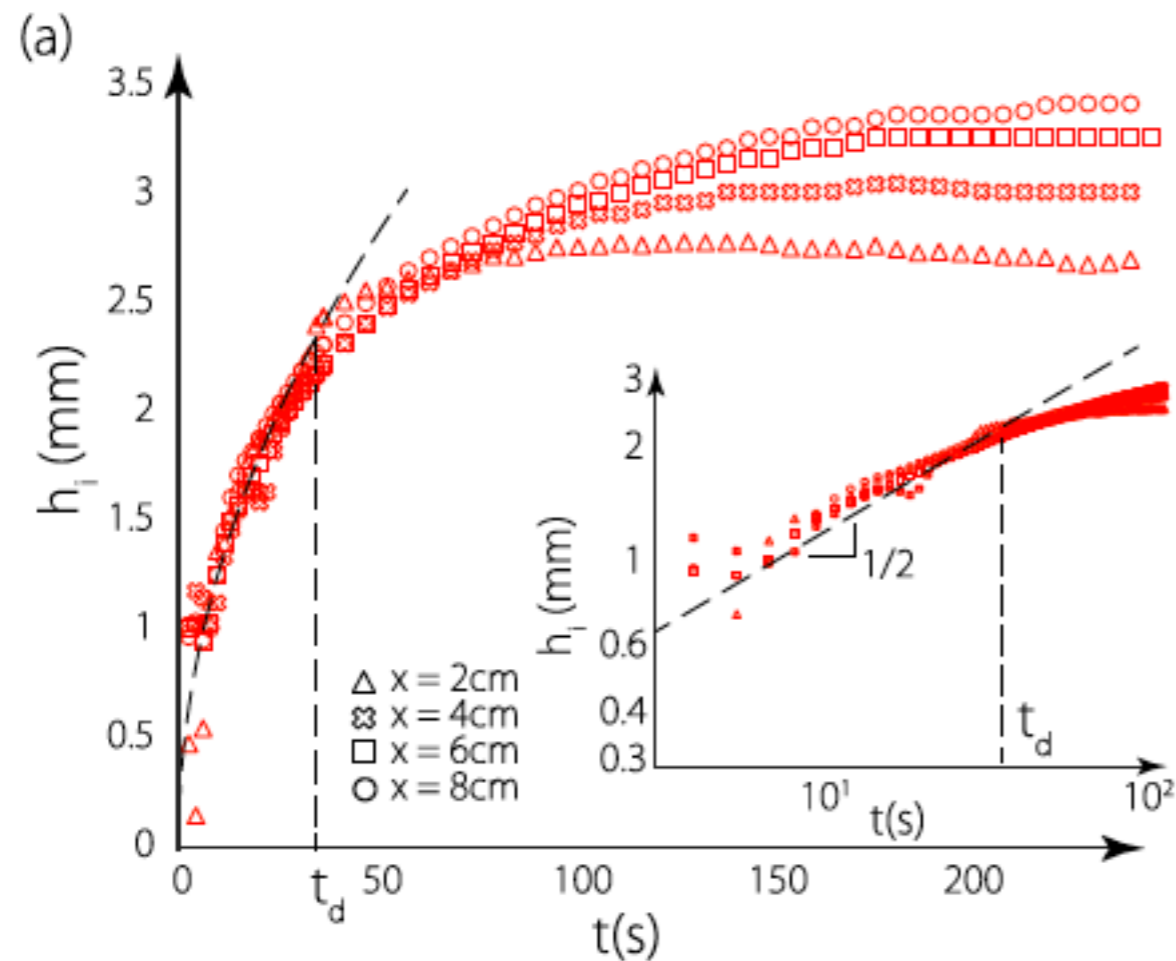


Freezing rivulet



The freezing rivulet problem, initial growth of ice layer



Write the heat transport equations in the substrate and solid phases (assume isothermal liquid phase).

Write the boundary conditions at the substrate/solid [$z=0$] and solid/liquid [$z=h(t)$] interfaces

Rewrite the equations with a rescaled space variable

Find the self-similar solutions of the heat equation

The freezing rivulet problem: physical parameters

Liquid water (at 0°C) :

thermal conductivity $\lambda_w = 0.6 \text{ W/m.K}$

heat capacity $C_w = 4.2 \cdot 10^3 \text{ J/kg.K}$

heat diffusivity $\kappa_w = 1.2 \cdot 10^{-7} \text{ m}^2/\text{s}$

Latent heat of freezing : $L = 3 \cdot 10^5 \text{ J/kg}$

Ice:

thermal conductivity $\lambda_i = 2 \text{ W/m.K}$

heat capacity $C_i = 2.0 \cdot 10^3 \text{ J/kg.K}$

heat diffusivity $\kappa_i = 1.12 \cdot 10^{-6} \text{ m}^2/\text{s}$

Substrate (copper):

thermal conductivity $\lambda_s = 400 \text{ W/m.K}$

heat capacity $C_s = 385 \text{ J/kg.K}$

heat diffusivity $\kappa_s = 1.2 \cdot 10^{-4} \text{ m}^2/\text{s}$