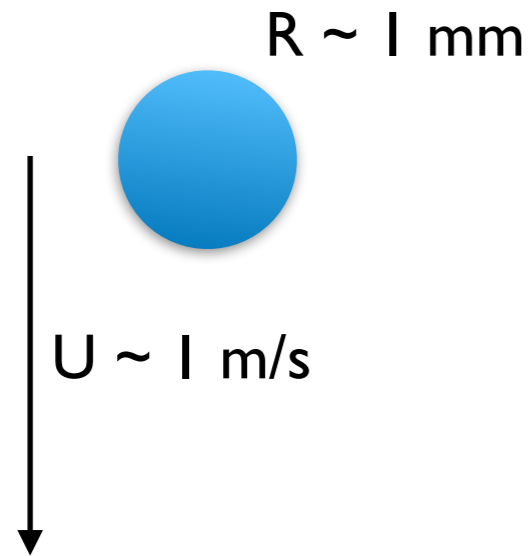
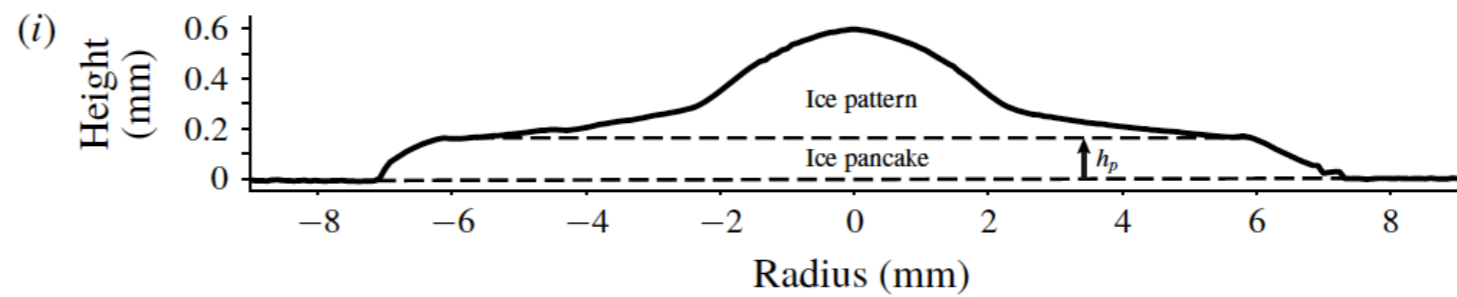
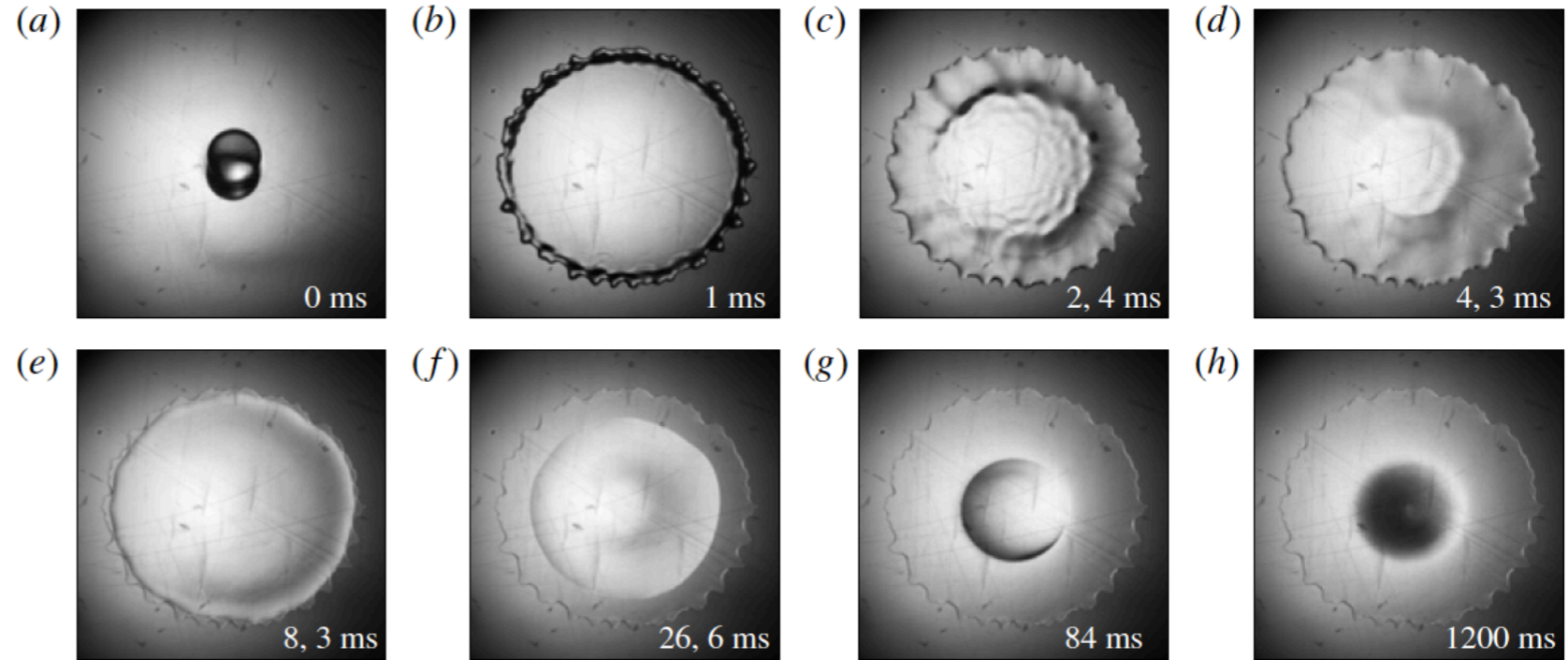


The freezing rain problem

$R = 1.9 \text{ mm}$
 $U = 2.6 \text{ m/s}$
 $T_s = -9^\circ \text{ C}$

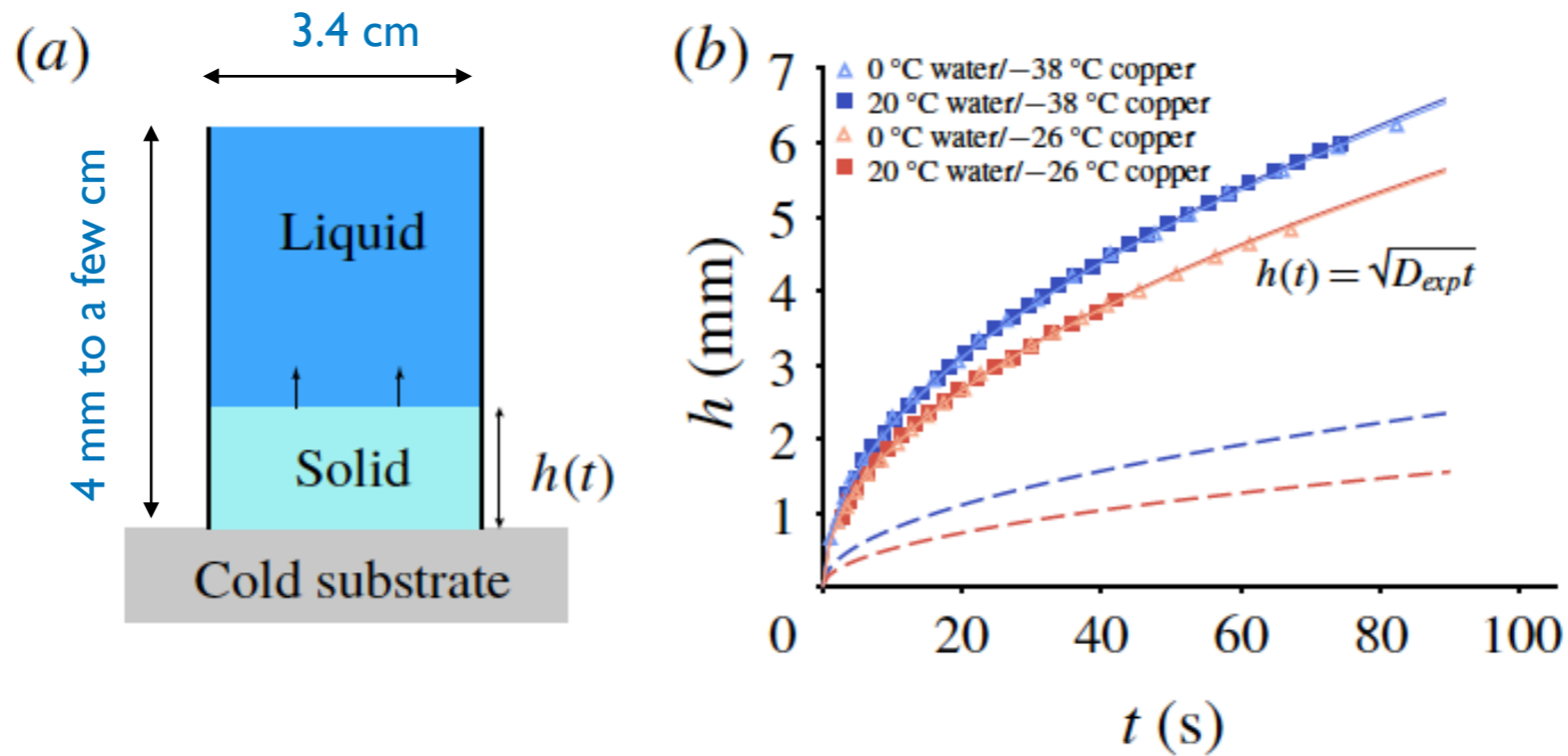


$T_s < T_f$



Final profile of frozen drop

The freezing rain problem: a simpler 1D geometry



Write the heat transport equations in the substrate and solid phases (assume isothermal liquid phase).

Write the boundary conditions at the substrate/solid [$z=0$] and solid/liquid [$z=h(t)$] interfaces

Rewrite the equations with a rescaled space variable

Find the self-similar solutions of the heat equation

The freezing rain problem: physical parameters

Liquid water (at 0°C) :

thermal conductivity $\lambda_w = 0.6 \text{ W/m.K}$

heat capacity $C_w = 4.2 \cdot 10^3 \text{ J/kg.K}$

heat diffusivity $\kappa_w = 1.2 \cdot 10^{-7} \text{ m}^2/\text{s}$

Latent heat of freezing : $L = 3 \cdot 10^5 \text{ J/kg}$

Ice:

thermal conductivity $\lambda_i = 2 \text{ W/m.K}$

heat capacity $C_i = 2.0 \cdot 10^3 \text{ J/kg.K}$

heat diffusivity $\kappa_i = 1.12 \cdot 10^{-6} \text{ m}^2/\text{s}$

Substrate (copper):

thermal conductivity $\lambda_s = 400 \text{ W/m.K}$

heat capacity $C_s = 385 \text{ J/kg.K}$

heat diffusivity $\kappa_s = 1.2 \cdot 10^{-4} \text{ m}^2/\text{s}$