

The coffee cup problem 2



How long does it take for the sucrose to diffuse to the top ?
At least weeks, months for a big cup.

How long does it take to cool down to room temperature ?

What if diffusion in air is the only mechanism ?

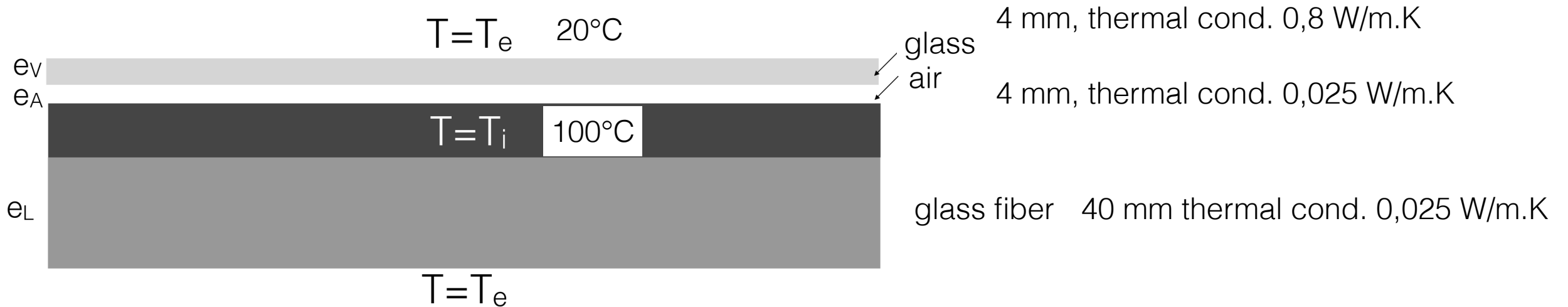
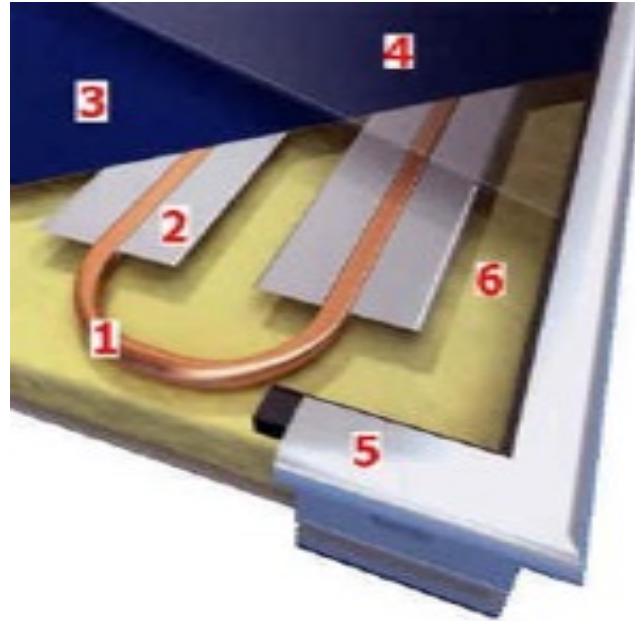
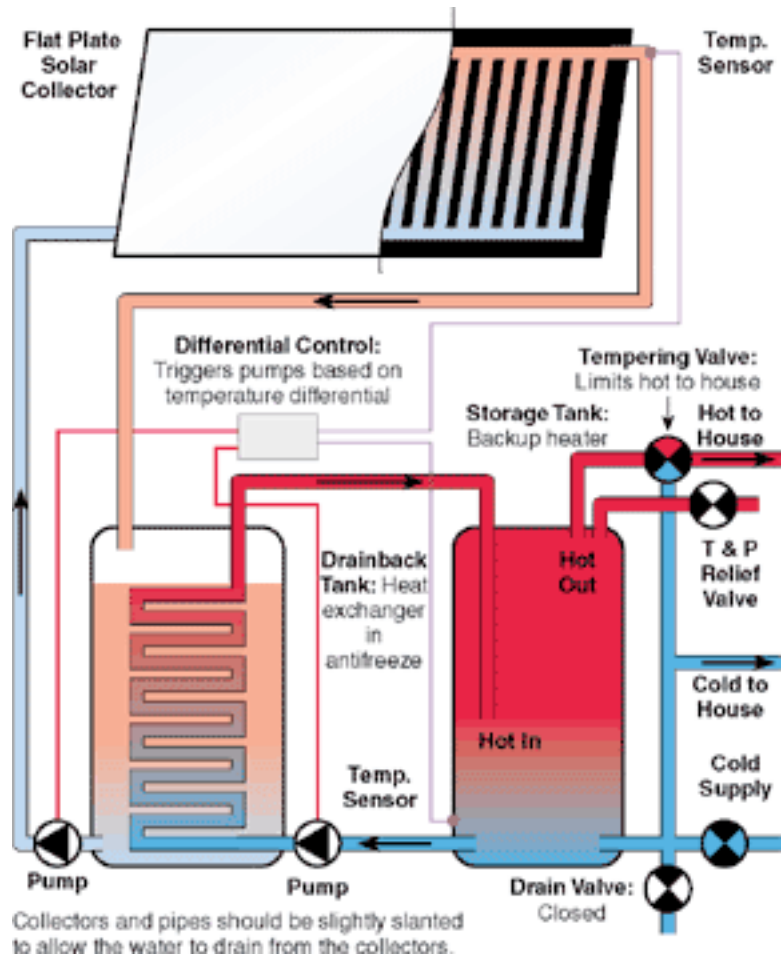
Physical properties of air :

density $\rho = 1 \text{ kg/m}^3$

specific heat $C_p = 1000 \text{ J/kg.K}$

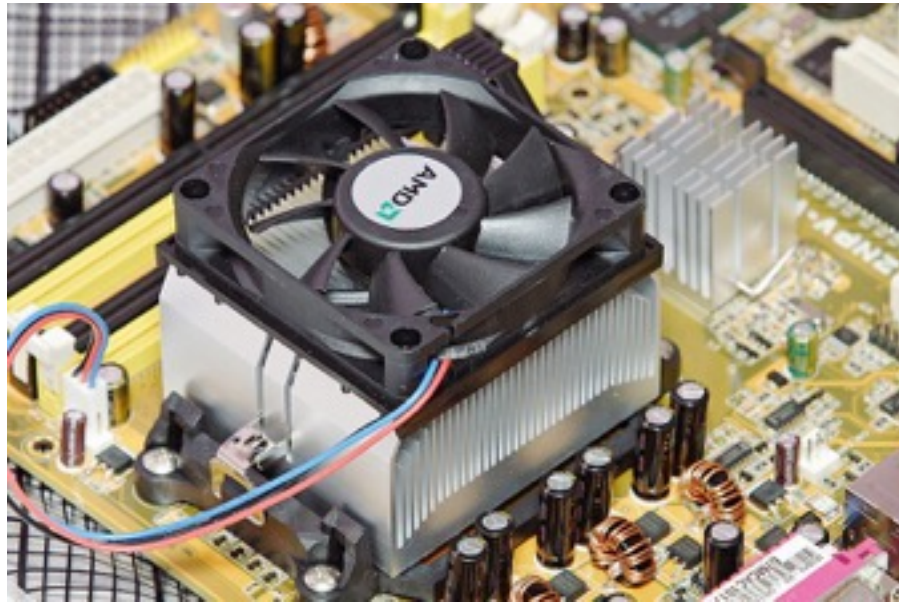
thermal conductivity $\lambda = 0.025 \text{ W/m.K}$

The solar heater problem I : how much heat do we lose from the collector ?



use the 1D steady state diffusion and the concept of thermal resistance to compute heat fluxes on both sides of the collector

The microprocessor problem 1 and 2



Power to dissipate : 50 W

Typical dimension : $L = 3\text{cm}$

Physical properties of air :

density 1 kg/m^3

specific heat 1000 J/kg.K

thermal conductivity 0.025 W/m.K

If we rely only on diffusion in air, how much power can we dissipate from the flat chip without fins?

how much power can we dissipate by adding a radiator with fins ?

is there an optimum length for fins given their thickness e and the heat transfer coefficient h between the fins and the surrounding air ?

Physical properties of aluminum (material of the fins) :

thermal conductivity 240 W/m.K

The Maurice Herzog problem I



How long can you stand on top of Annapurna without gloves ? (no wind)

use the 1D bioheat equation to determine the temperature in Maurice's fingers (3mm of tissue between bone and skin) at steady state

steady state 1D diffusion + source term

blood flow rate per unit volume of tissue: V_b 10^{-4} s^{-1}

blood density: ρ_b 1000 kg/m^3

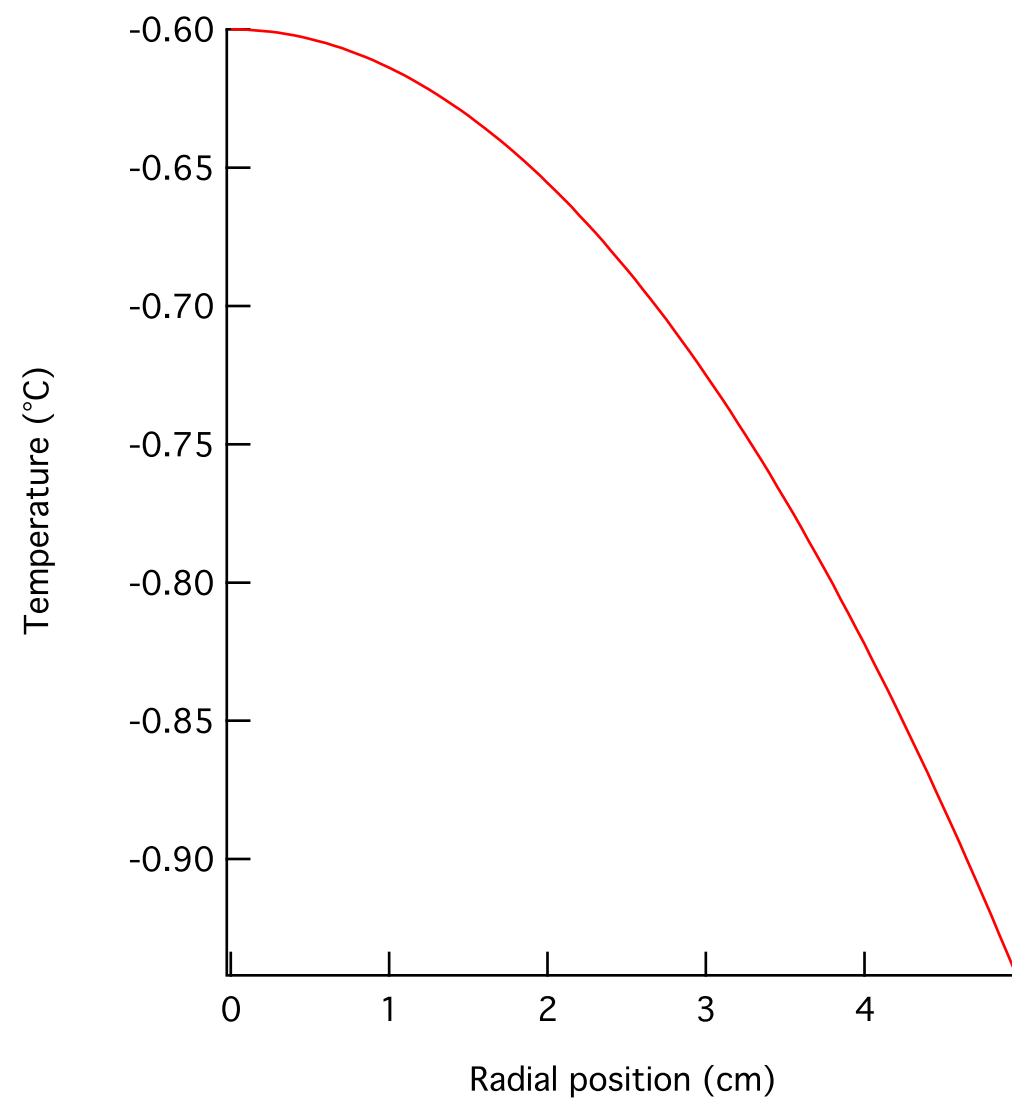
blood specific heat: C_b 3600 $J/kg.K$

thermal conductivity of tissue: λ 0.5 $W/m.K$

metabolic heat generation rate: q_m 700 W/m^3

outside temperature: T_e $-20^\circ C$

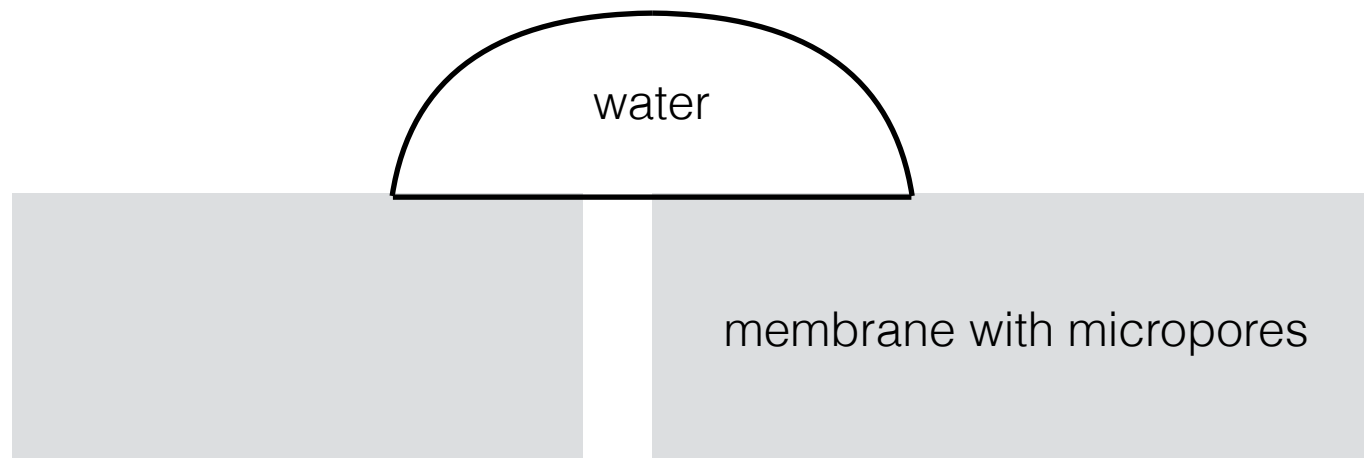
heat transfer coefficient with air: h 2 $W/m^2.K$



The Alex Thomson problem



how much water vapor is permeating through his clothing ?



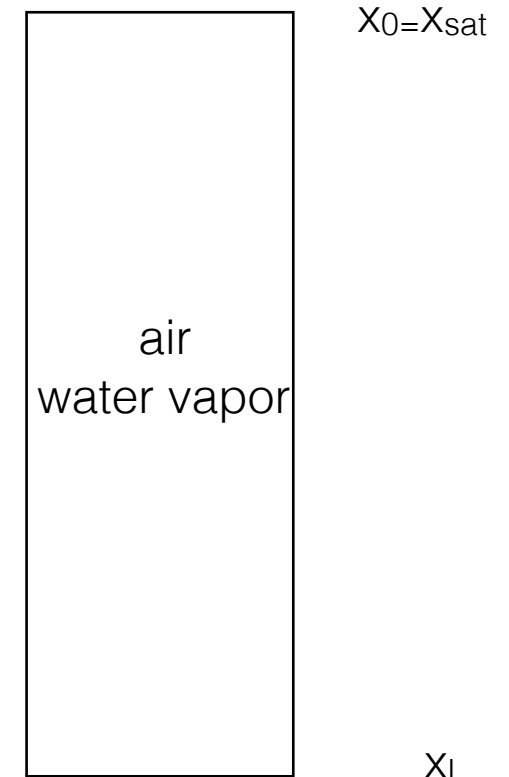
water vapor $\phi\%$

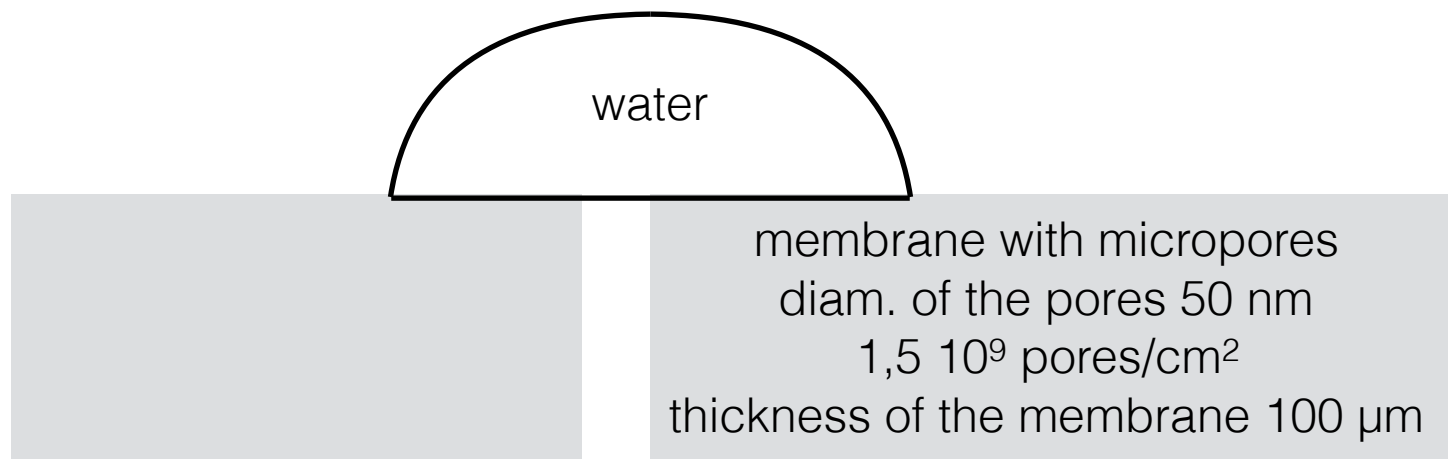
$$X_0 = X_{\text{sat}} = \frac{p_{\text{sat}}}{p}$$

$$X_L = \phi X_{\text{sat}} = \phi \frac{p_{\text{sat}}}{p}$$

$$p_{\text{sat}} = 0.03 \text{ bar at } 298 \text{ K}$$

$$D = 0.25 \cdot 10^{-4} \text{ m}^2/\text{s}$$





water vapor $\phi\%$

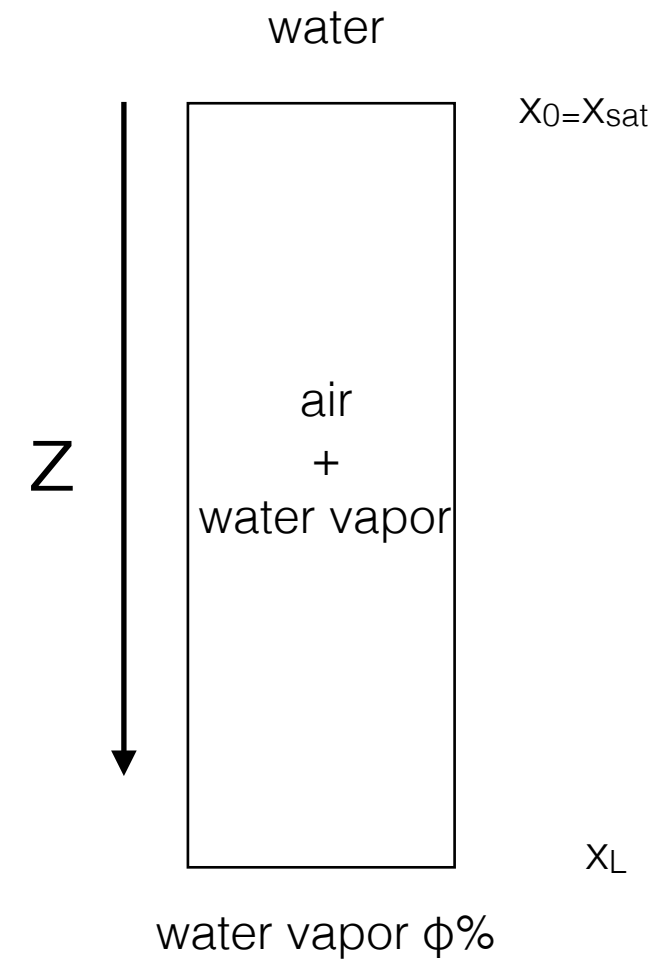
$$X_{A0} = X_{\text{sat}} = p_{\text{sat}}/p$$

$$X_{AL} = \phi X_{\text{sat}} = \phi p_{\text{sat}}/p$$

$$p_{\text{sat}} = 0.03 \text{ bar at } 298 \text{ K}$$

$$D_A = 0.25 \cdot 10^{-4} \text{ m}^2/\text{s}$$

the mixture A+B is treated as an ideal gaz mixture



Write the molar fluxes of vapor N_A and air N_B as a function of molar fractions x_A and x_B

$$d N_A/dz = ? \quad d N_B/dz = ? \quad \text{value of } N_B \text{ at the gaz/water interface ?}$$